

Study of chargino-neutralino production at hadron colliders in a long-lived slepton scenario

Ryuichiro Kitano (LANL)

Based on 0806.1057 [hep-ph]

Motivation

A standard assumption of SUSY phenomenology: neutralino LSP

- Why?
1. explains dark matter of the universe.
 2. The Bino tends to be light due to a negative quantum correction.

But the **gravitino LSP** with **stau NLSP** is equally plausible.

1. explains dark matter of the universe.
2. The stau tends to be light due to a negative quantum correction through the Yukawa interaction.

Actually, the scenario of the thermal relic neutralino as dark matter has a **big problem**.

Bino LSP --> We must assume gravity mediation.

- ▶ There is **always** a singlet field to give a mass to gauginos. The potential of the singlet field cannot be stabilized in a supersymmetric way to carry a SUSY breaking VEV.
- ▶ Moduli problem!!! (Moduli decay too late and/or overproduce gravitinos.)
- ▶ **Inconsistent** with the assumption in the thermal relic calculation. We need to carefully arrange the inflation sector such that moduli domination doesn't happen.

It's **dangerous** to believe that SUSY signatures at the LHC involves missing ET by neutralinos.

Overview of stau NLSP at LHC

[Drees, Tata '90][Feng, Moroi '97]
[Nisati, Petrarca, Salvini '97][Martin, Wells '98]
[Hinchliffe, Paige '98][Polesello, Rimoldi '99]
[Ambrosanio, Mele, Petrarca, Polesello, Rimoldi '00]

If the gravitino mass is large enough ($\gg 100\text{keV}$), staus decay outside the detector.
Stau looks like a **muon** which is a very nice particle for collider physics!

Very accurate mass ($\pm 10\text{-}100\text{MeV}$) and momentum measurement (a few %) are possible at ATLAS (and probably at CMS).

[Polesello, Rimoldi '99][Ambrosanio, Mele, Petrarca, Polesello, Rimoldi '00]

→ **Lots of applications!**

* Neutralino (and other sparticle) mass measurement

[Hinchliffe, Paige '98][Ellis, Raklev, Oye '06][Ibe, RK '06]

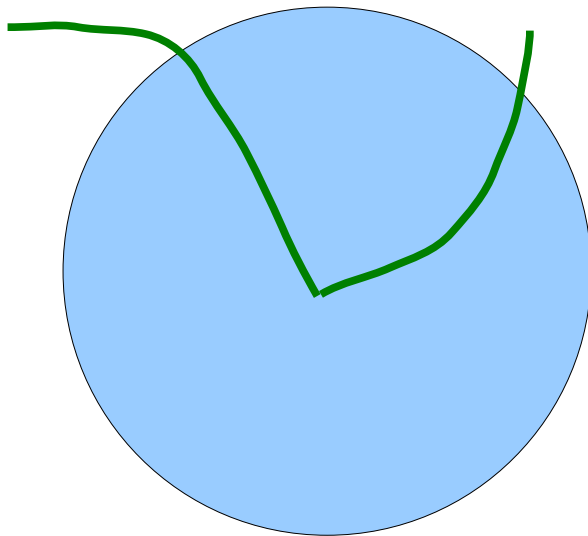
* Spin measurement

[Rajaraman, Smith '07]

* lifetime measurement

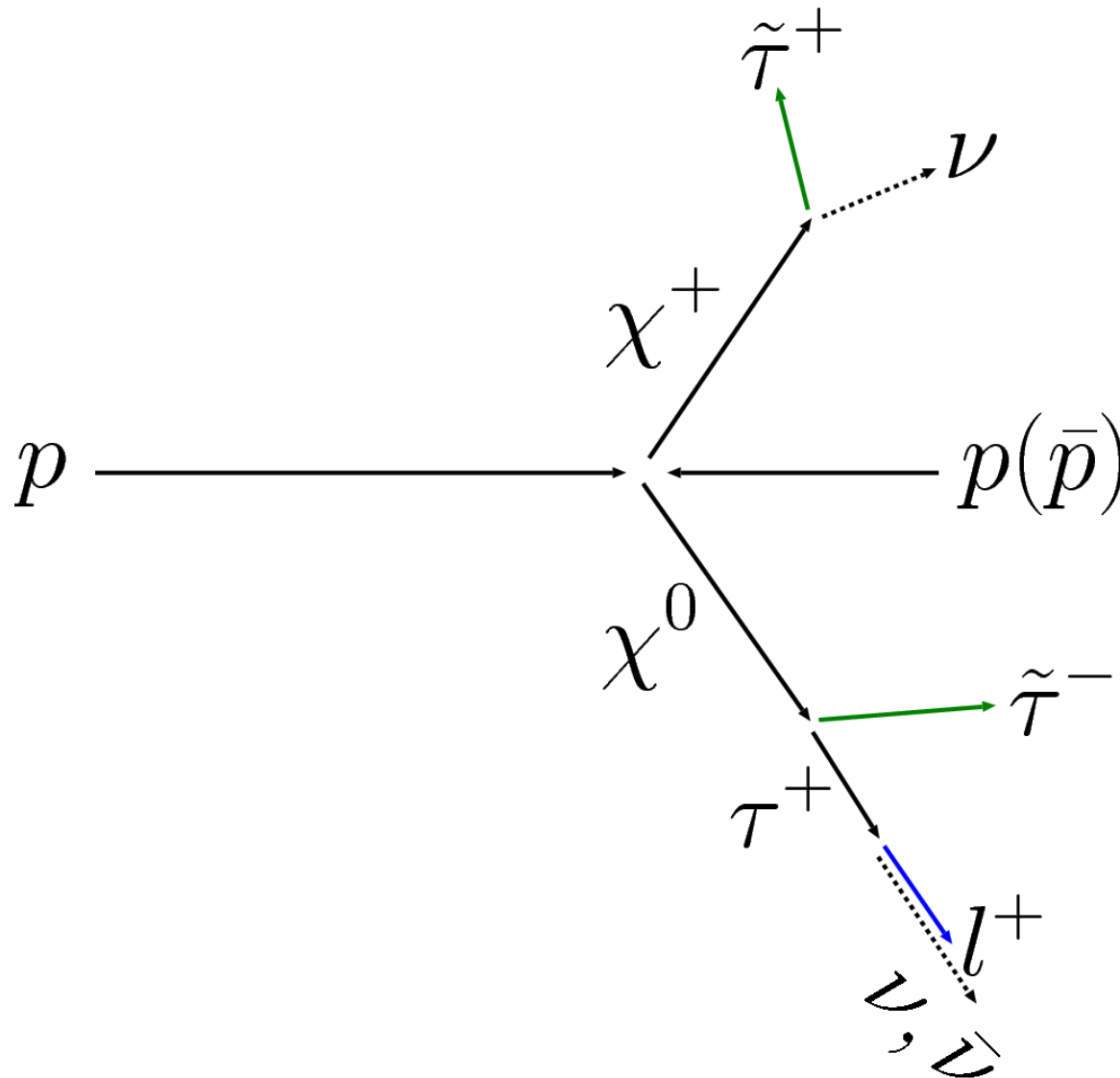
[Buchmuller, Hamaguchi, Ratz, Yangida '04]

[Hamaguchi, Kuno, Nakaya, Nojiri '04][Feng, Smith '04]



Chargino-neutralino production with long-lived stau

With long-lived staus in the final state, we can do studies of exclusive processes at hadron colliders just like at a [Linear Collider](#)!



This process has a [purely leptonic](#) final state. Clean!

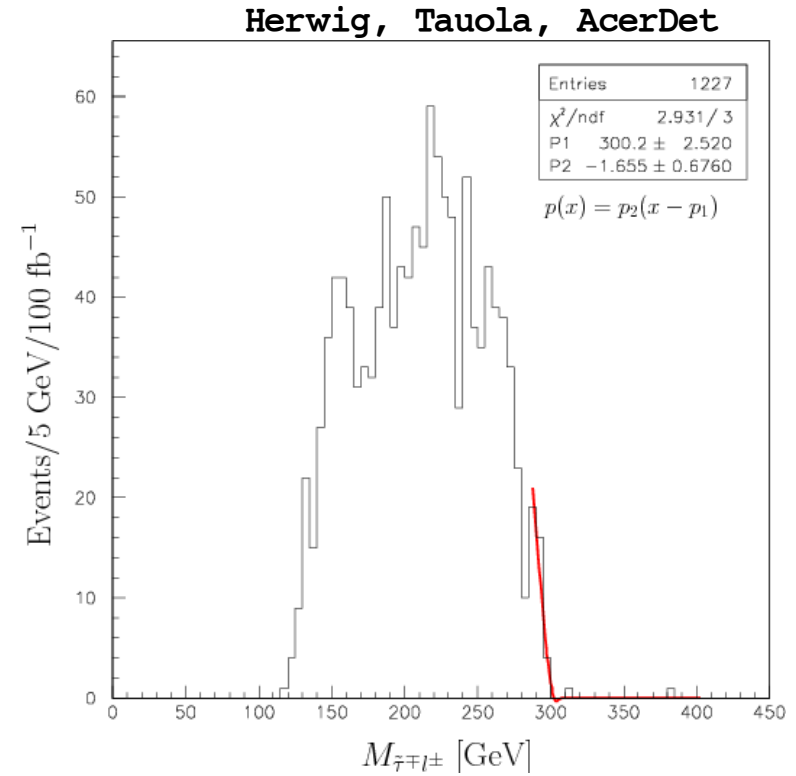
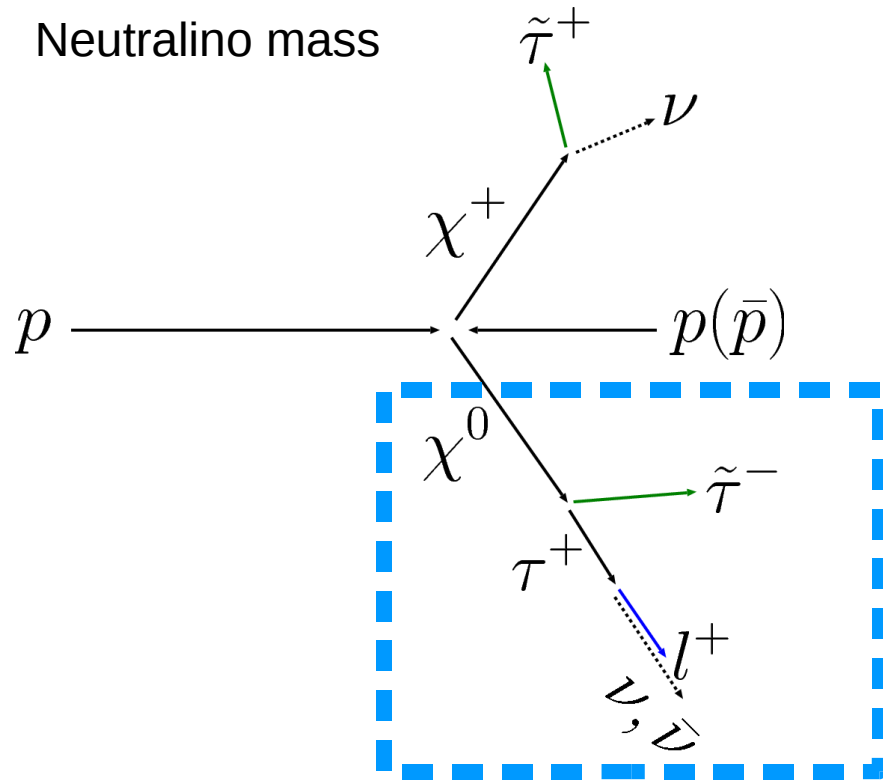
If we know the neutralino and chargino masses, we can [fully reconstruct](#) the event up to a two-fold ambiguity.

We can do many things!

- * mass measurements
- * spin measurements
- * P violation measurements
- * CP violation measurements

They are going to be [excellent tests of supersymmetry!!!](#)

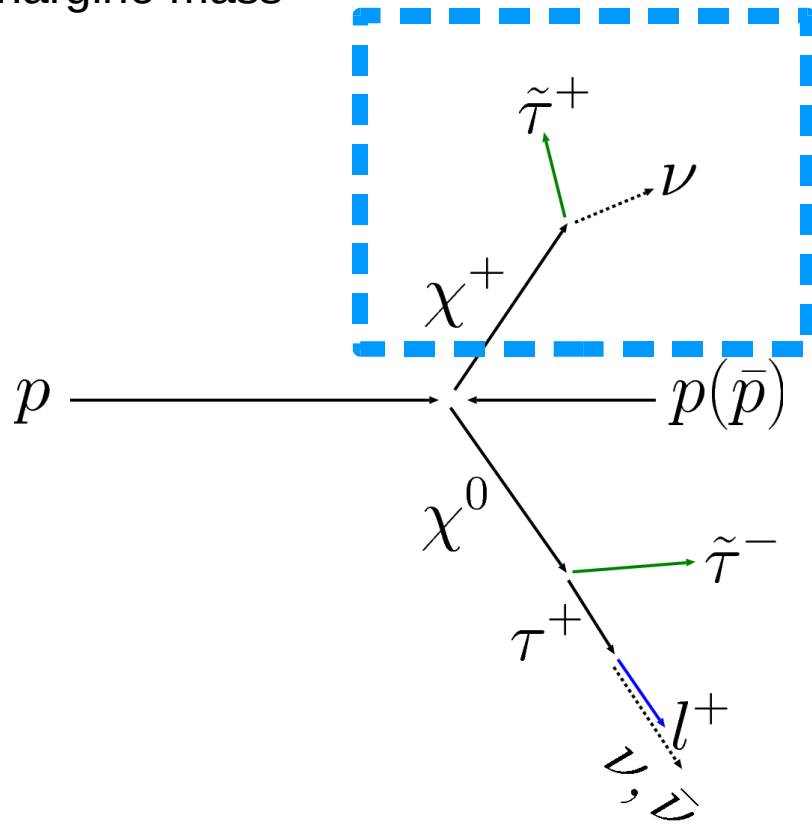
Mass measurements



$\delta M = 3$ GeV

(Pure Higgsino model with $\mu = 300$ GeV
and right-handed $m(\text{stau}) = 109$ GeV)

Chargino mass



Once we know the neutralino mass, we know the rescaling factor of the lepton momentum.

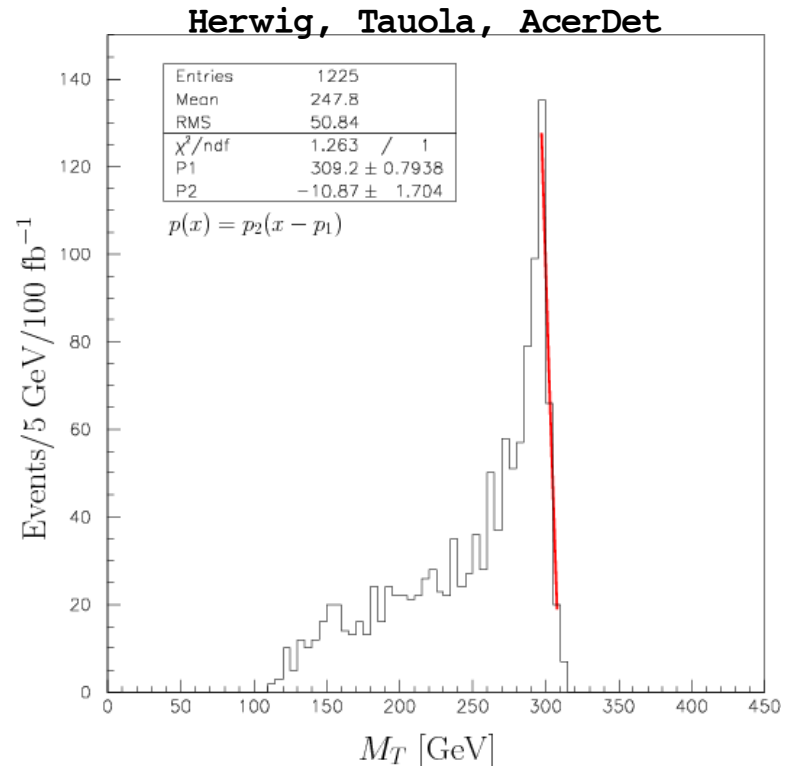
$$z_l \equiv \frac{E_l}{E_\tau}, \quad \left(P_{\tilde{\tau}^-} + \frac{P_l}{z_l} \right)^2 = m_{\chi^0}^2$$

→ Transverse momentum of the neutrino from the chargino decay can be solved.

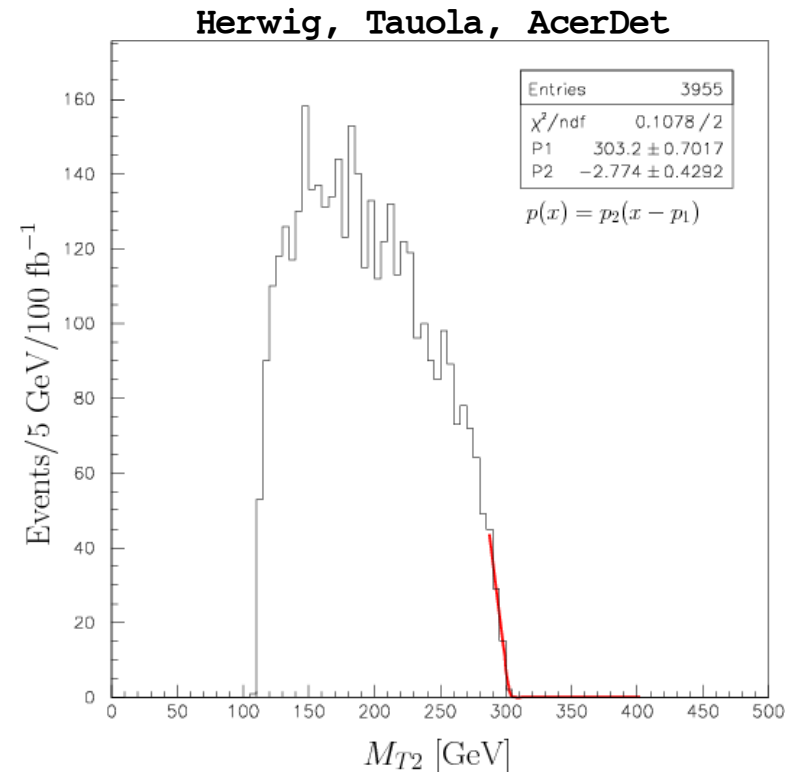
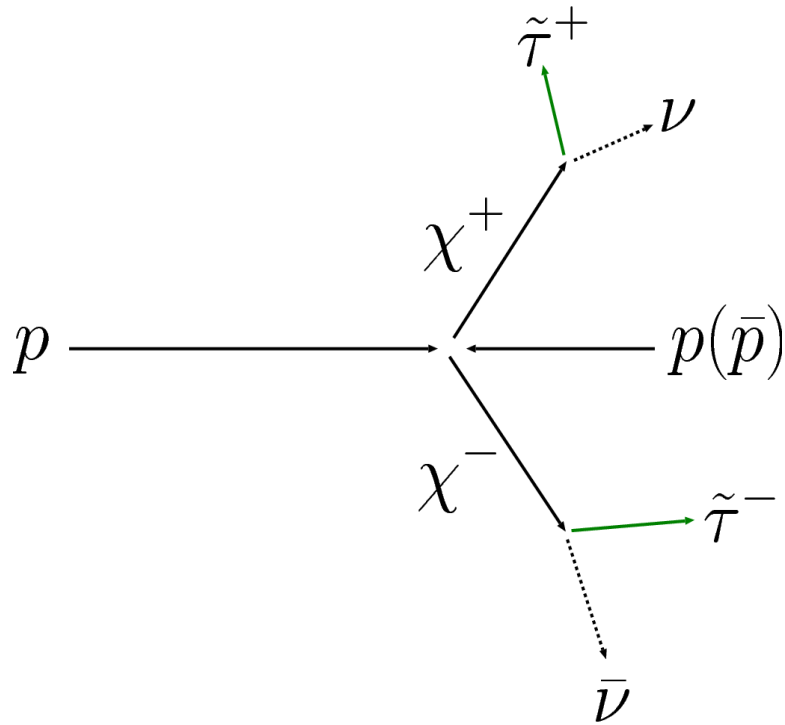
→ Transverse mass

$$\delta M = 0.8 \text{ GeV}$$

(although it will depend on the resolution of the missing momentum measurement.)



By the way, the chargino mass can also be measured by using chargino-pair production events.

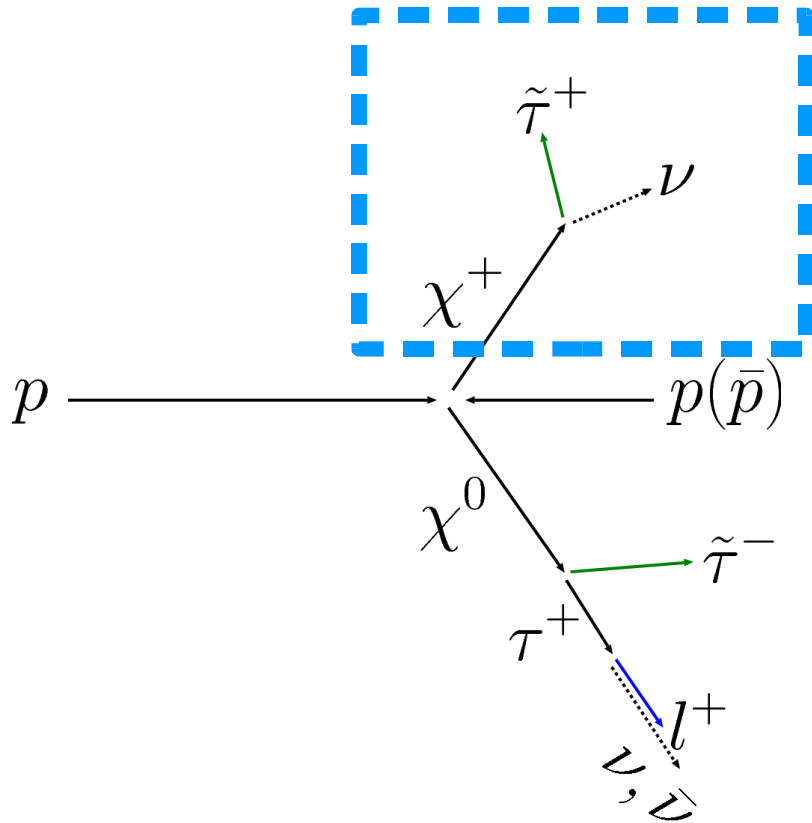


The M_{T2} variable can be used for this process.

[Lester, Summers '99]

This method directly measures the chargino mass.

Now with the knowledge of the chargino mass, z-direction of the neutrino momentum from the chargino decay can be solved:



$$(P_{\tilde{\tau}^+} + P_{\nu})^2 = m_{\chi^+}^2$$

Unfortunately, we have **two solutions** to this equation.

But anyway, we can **fully reconstruct** the event **up to a two-fold ambiguity** once the neutralino and chargino masses are known.

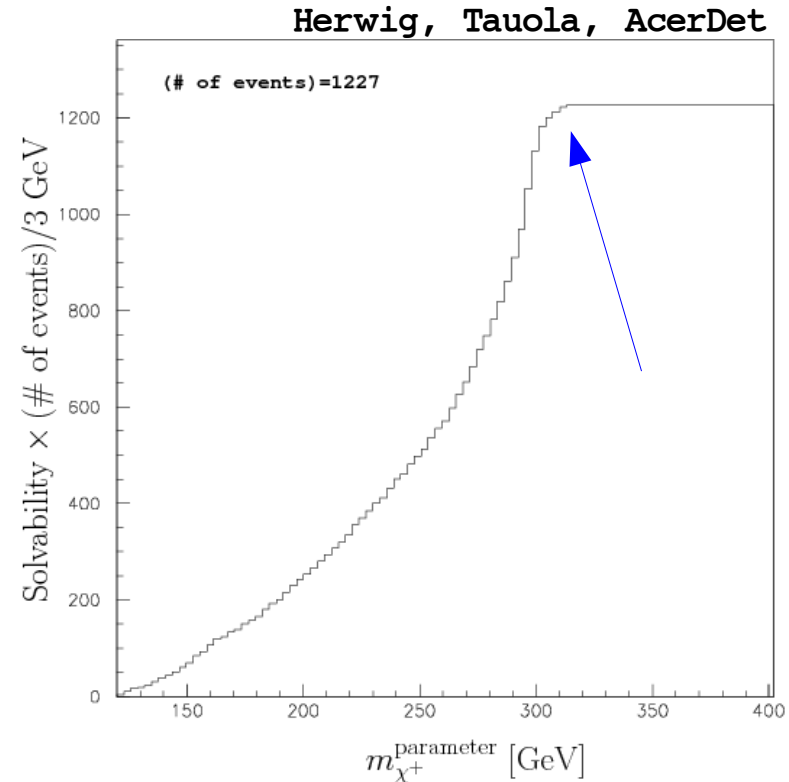
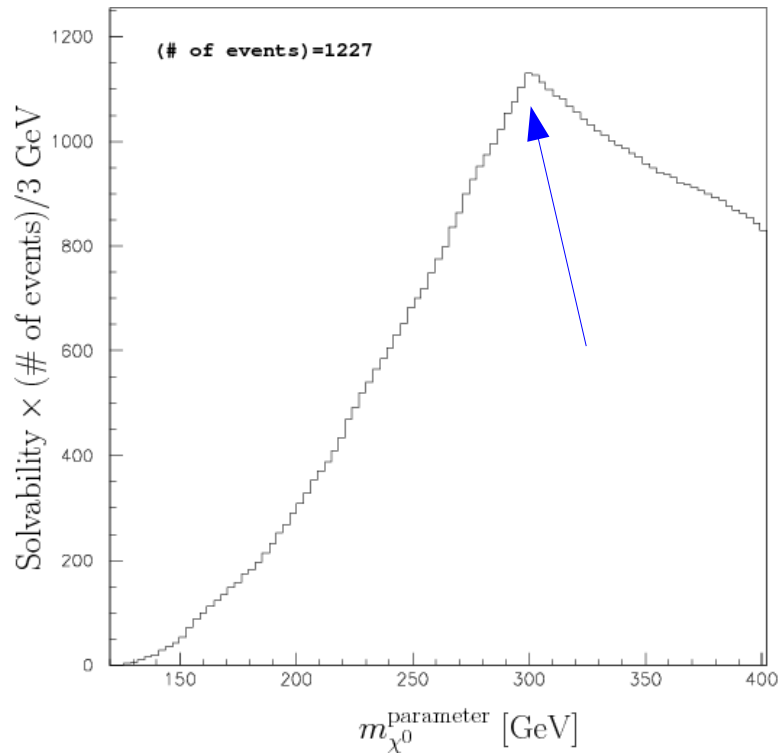
In this situation, we can do mass measurement in a more direct method.

Solvability analysis for neutralino and chargino masses

[Kawagoe, Nojiri, Polsello '04]

[Davis et al, (CMS collaboration) '06]

[Cheng, Gunion, Han, Marandella, McElrath '07]



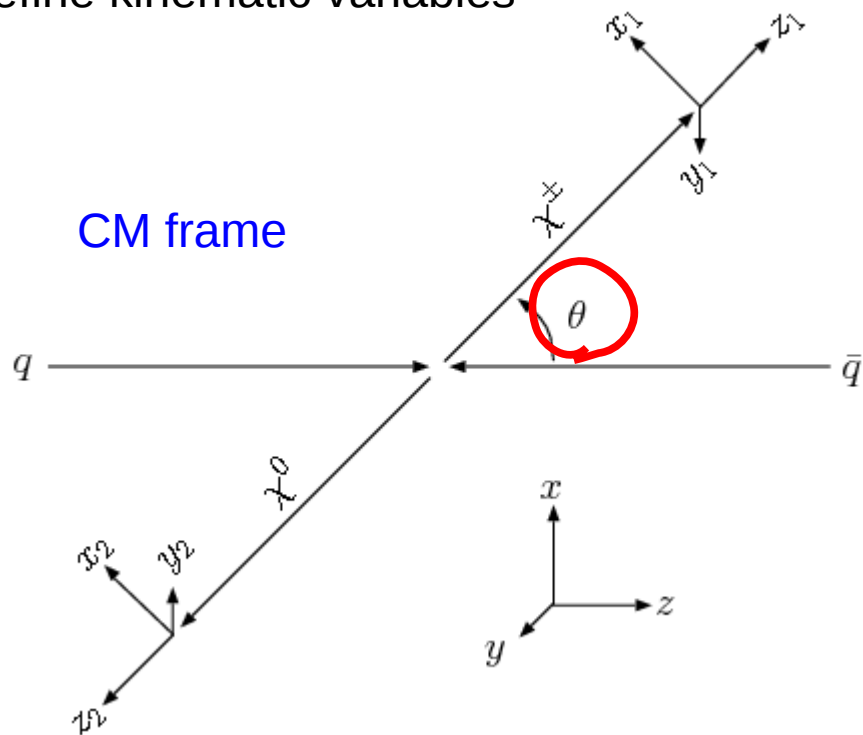
Try to solve kinematics with various input masses. Solvability is defined as the probability to have a physical solution, i.e., $P_z(v)$ is a real number and $0 < |z| < 1$.

By looking for a **peak** or a **point where solvability saturates**, we can get masses.

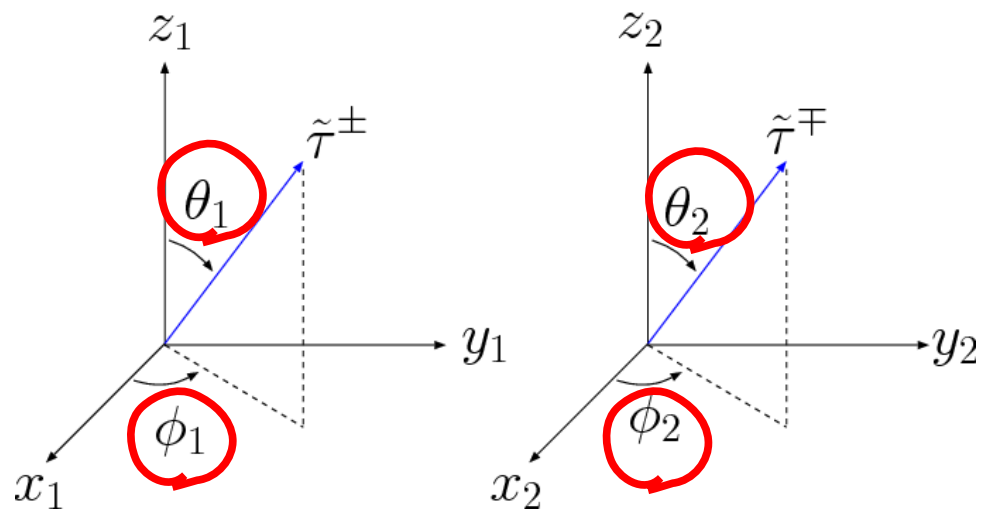
$\delta M \sim$ a few GeV.

Various distributions

Define kinematic variables



Rest frame of chargino



Rest frame of neutralino

Lepton energy fraction in leptonic tau decay

$$z_l \equiv \frac{E_l}{E_\tau}, \quad 0 \leq z_l \leq 1$$

There are six kinematic variables.

The cross section formula

The formula is pretty simple.

$$d\sigma \propto \frac{d \cos \theta}{2} \frac{d\Omega_1}{4\pi} \frac{d\Omega_2}{4\pi} dz_l \sum_{a,b=0}^3 \underbrace{D_A^a(\theta_1, \phi_1)}_{\text{chargino decay}} \rho^{ab}(\theta) \underbrace{\widetilde{D}_B^b(\theta_2, \phi_2, z_l)}_{\text{neutralino decay}}$$

chargino-neutralino production

Spin correlations

$$\widetilde{D}_B^b(\theta_2, \phi_2, z_l) = \frac{1}{3}(1 - z_l) \left[(5 + 5z_l - 4z_l^2) D_B^b(\theta_2, \phi_2) - \underbrace{a_N}_{\text{red wavy}} (1 + z_l - 8z_l^2) \delta^{b0} \right]$$

$$D_A^a = \begin{pmatrix} 1 \\ \pm \underbrace{a_C}_{\text{red wavy}} \sin \theta_1 \cos \phi_1 \\ \pm \underbrace{a_C}_{\text{red wavy}} \sin \theta_1 \sin \phi_1 \\ \pm \underbrace{a_C}_{\text{red wavy}} \cos \theta_1 \end{pmatrix}, \quad D_B^b = \begin{pmatrix} 1 \\ \mp \underbrace{a_N}_{\text{red wavy}} \sin \theta_2 \cos \phi_2 \\ \mp \underbrace{a_N}_{\text{red wavy}} \sin \theta_2 \sin \phi_2 \\ \mp \underbrace{a_N}_{\text{red wavy}} \cos \theta_2 \end{pmatrix} \leftarrow \text{spin summed part}$$

$$\rho^{ab}(\theta) = \dots \leftarrow \text{All the components are non-vanishing.}$$

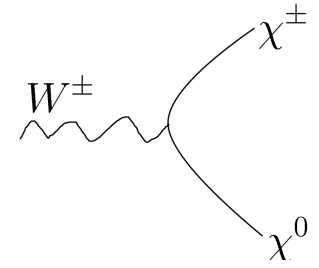
a_C and a_N are **parity asymmetry parameter** ($-1 < a < 1$) in the chargino decay and the neutralino decay, respectively. Non-trivial angular distribution measures parity violation.

$a_C = 1$ because neutrino has always the left-handed chirality (maximal parity violation).

Lagrangian and asymmetry parameters

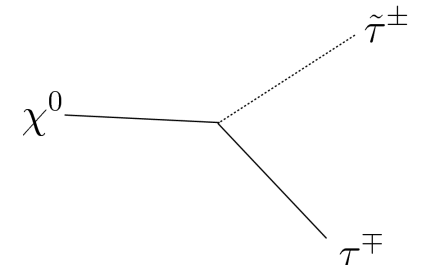
* Chargino-neutralino production:

$$\mathcal{L}_W = \bar{\chi}^0 \gamma^\mu (w_L P_L + w_R P_R) \chi^- W_\mu^+ + \text{h.c.}$$



* neutralino decay:

$$\mathcal{L}_{\chi^0} = \bar{\chi}^0 (n_R P_R + n_L P_L) \tau \tilde{\tau}^\dagger + \text{h.c.}$$



$$a_N \equiv \frac{|n_L|^2 - |n_R|^2}{|n_L|^2 + |n_R|^2}$$

← Parity violation in neutralino decay

$$a_W \equiv \frac{|w_L|^2 - |w_R|^2}{|w_L|^2 + |w_R|^2}$$

Parity violation in production

$$\xi_W \equiv \frac{2\text{Re}[w_L^* w_R]}{|w_L|^2 + |w_R|^2}$$

$$\eta_W \equiv \frac{2\text{Im}[w_L^* w_R]}{|w_L|^2 + |w_R|^2}$$

CP violation in production

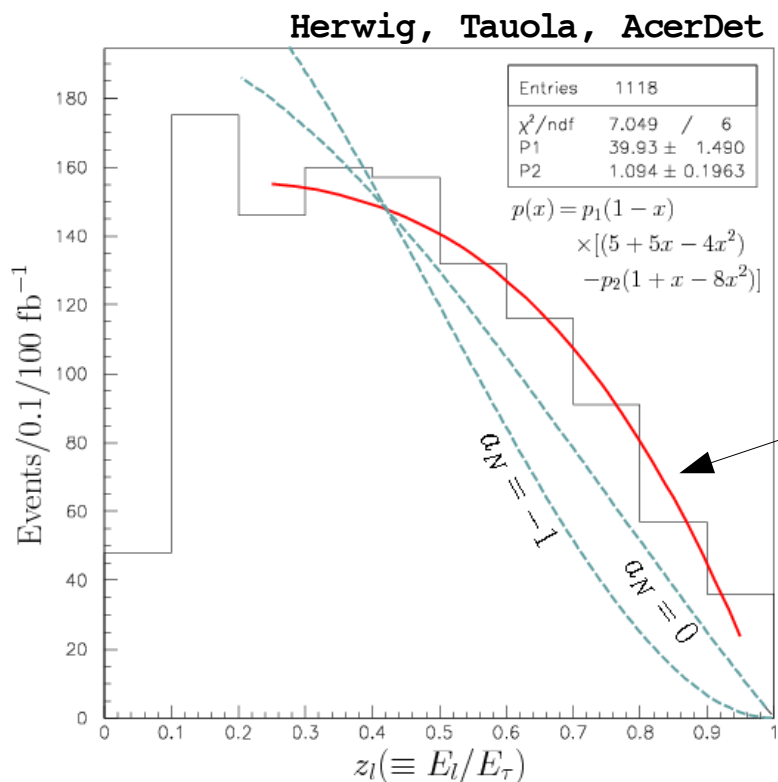
Z_l distribution

z_l is a simple observable since it is a **boost invariant** quantity.
We can measure it in the lab frame. There is **no two-fold ambiguity**.

$$d\sigma \propto \frac{1}{3}(1 - z_l) \left[(5 + 5z_l - 4z_l^2) - a_N(1 + z_l - 8z_l^2) \right] dz_l$$

This is a well-known distribution of the polarized tau decay. [Bullock, Hagiwara, Martin '93]
This is true for both $\chi+\chi_0$ and $\chi-\chi_0$ productions.

Again, in the **pure Higgsino** with **right-handed stau** model,



τ is left-handed

Theory value is $a_N=1$. We can distinguish from other models.

$$a_N = 1.1 \pm 0.2$$

In general, this parameter has information on the **LR mixing of the stau** and the **gaugino/higgsino mixing**.

Polar angle distributions

Again, the same formula for both $\chi+\chi_0$ and $\chi-\chi_0$ productions.

$$d\sigma \propto [1 + a_W \langle f_1(\beta_A, \beta_B) \rangle \cos \theta_1 + a_W a_N \langle f_1(\beta_B, \beta_A) \rangle \cos \theta_2 + a_N \langle f_2(\beta_A, \beta_B) \rangle \cos \theta_1 \cos \theta_2] \frac{d \cos \theta_1}{2} \frac{d \cos \theta_2}{2}$$

$$0 < f_1 < 1$$

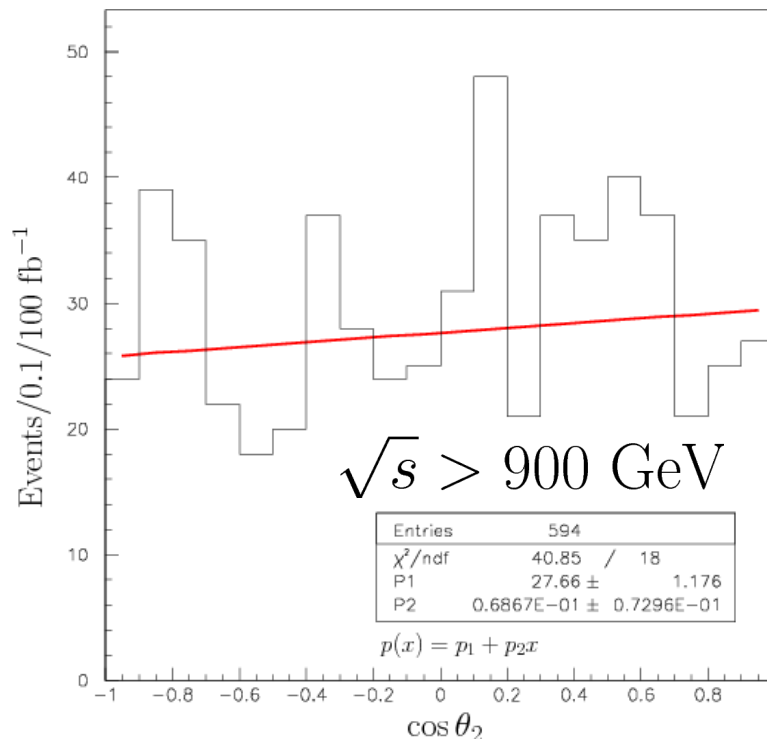
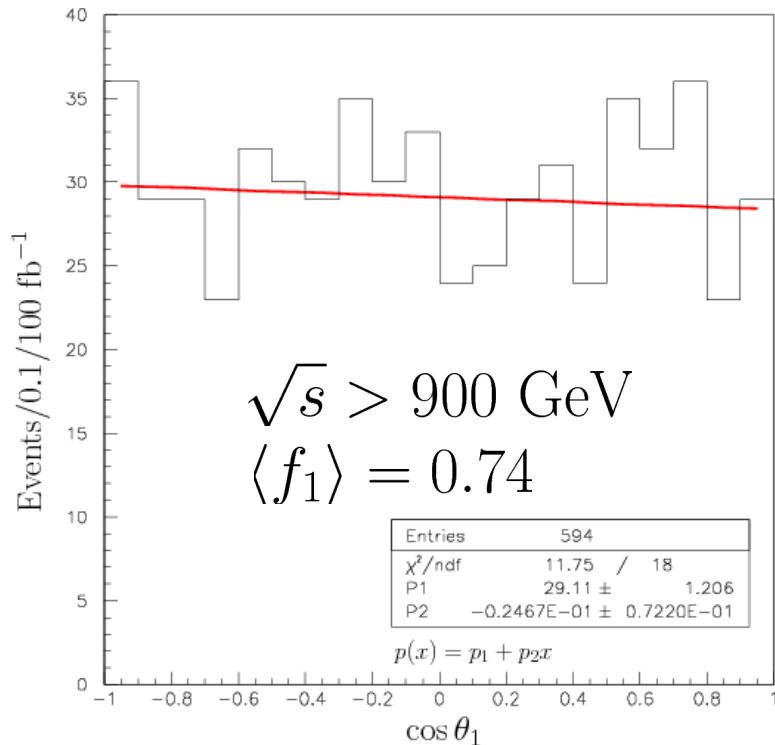
Threshold production

Boosted production

$$1/3 < f_2 < 1$$

Boosted production

Threshold production



Theoretical value:

$$a_W = 0$$

→ Flat distribution

False solutions are under control. Those are randomly distributed.

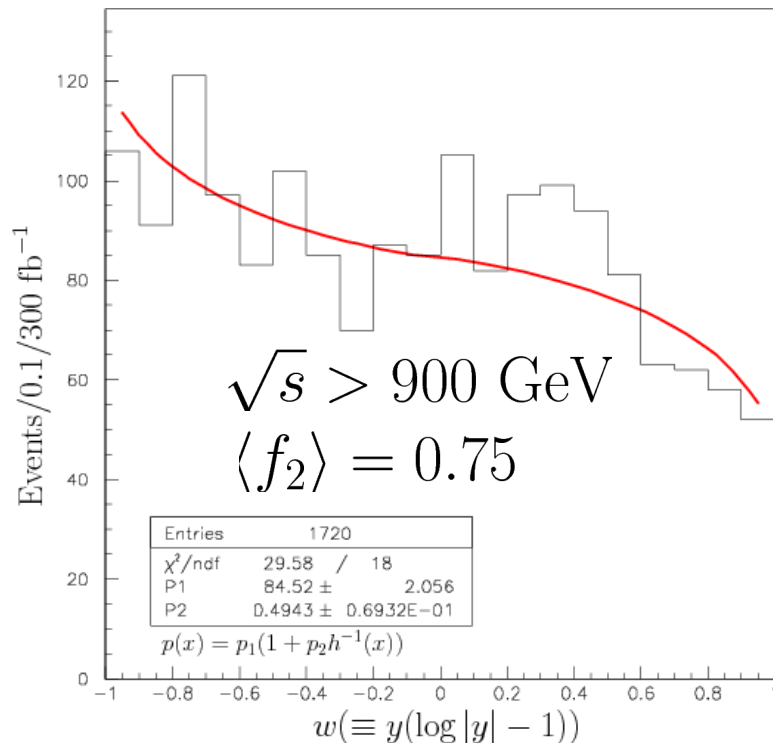
Angle-angle correlation

The $\cos\theta_1\cos\theta_2$ term gives a non-trivial correlation even if $a_W=0$.

By defining a variable:

$$w = h(y) \equiv y(\log y - 1) \quad y \equiv \cos \theta_1 \cos \theta_2$$

$$\rightarrow d\sigma \propto (1 + a_N \langle f_2 \rangle h^{-1}(w)) dw$$



Deviation from the flat distribution is a sign of **parity violation** and the **spin-spin correlation**.

The non-trivial distribution is diluted by false solutions by about a factor of two.

Combine with the a_N measurement by $Z1$ distribution, this will be an interesting test of spins!

$$d\sigma \propto \left[1 \pm \frac{\pi^2}{16} \langle g_1(\beta_A, \beta_B) \rangle \cos \phi_1 \pm \frac{\pi^2}{16} \eta_W \langle g_2(\beta_A, \beta_B) \rangle \sin \phi_1 \right] \frac{d\phi_1}{2\pi}$$

$$d\sigma \propto \left[1 \mp \frac{\pi^2}{16} a_N \langle g_1(\beta_B, \beta_A) \rangle \cos \phi_2 \mp \frac{\pi^2}{16} a_N \eta_W \langle g_2(\beta_B, \beta_A) \rangle \sin \phi_2 \right] \frac{d\phi_2}{2\pi}$$

$\sin\phi$ term measures **CP (or T)** violation.

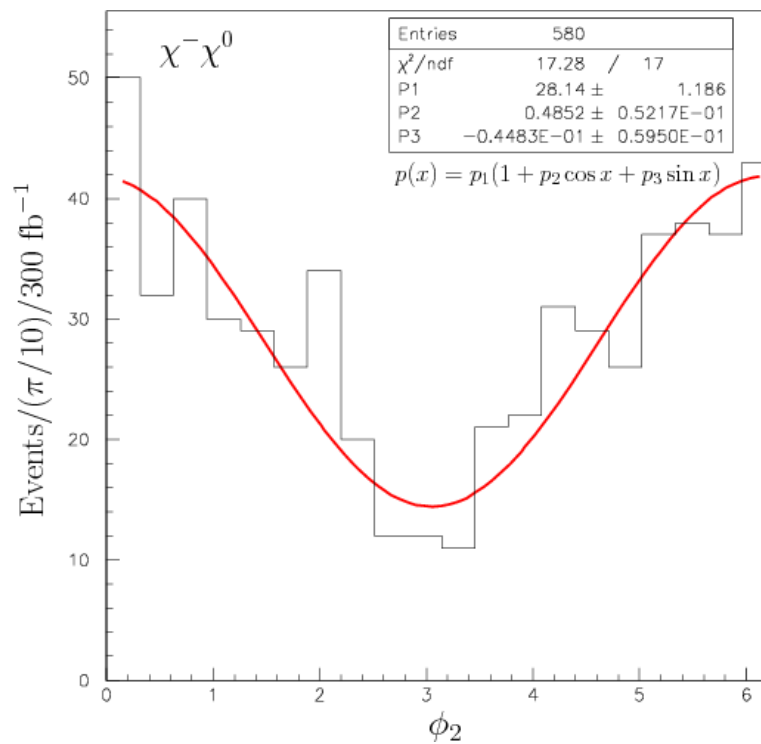
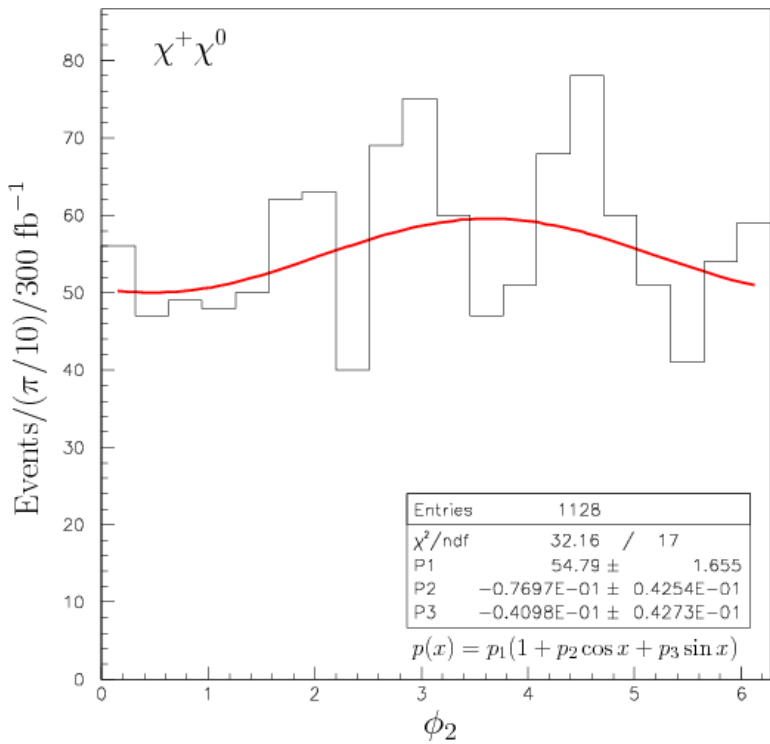
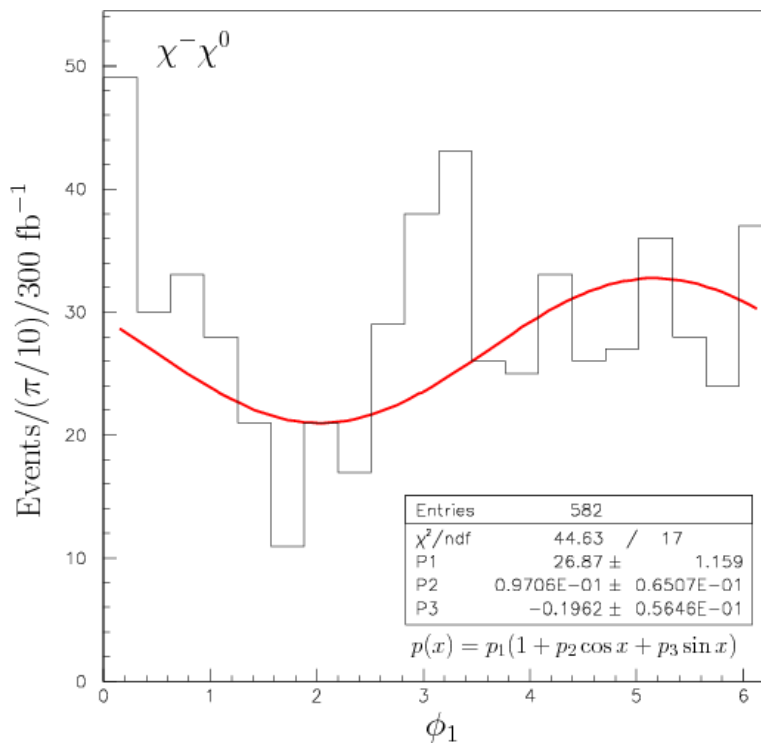
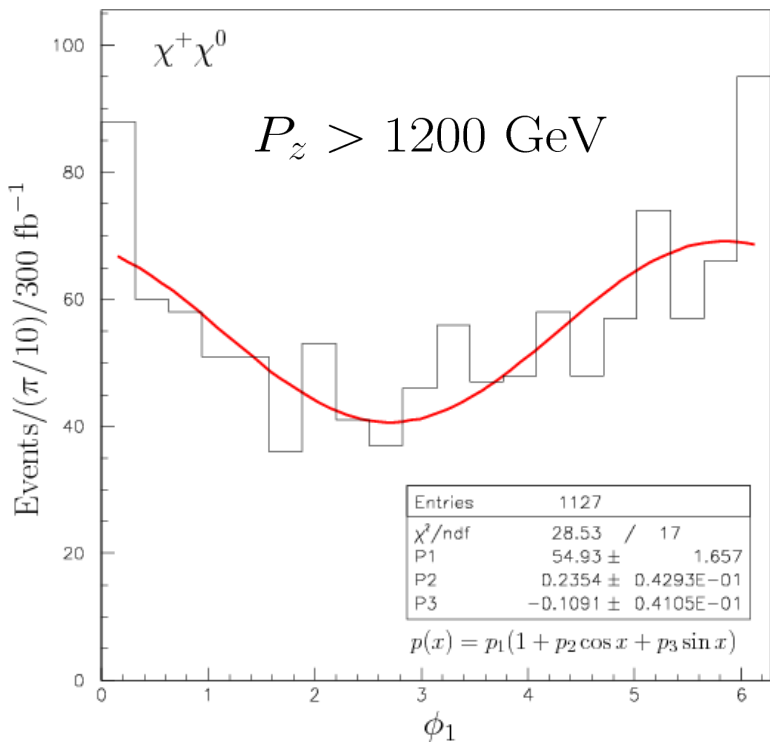
Signs of the coefficients are opposite for $\chi+\chi_0$ and $\chi-\chi_0$ productions.

Effective polarization of the beam through the W-quark interaction and the **parity violation in the decays** make the distribution possible.

We need to know the **direction of the initial (anti-)quark** to define the azimuthal angle. (we know it only statistically at the LHC.)

$0 < g_1 < 1$
 boosted production threshold production

$0 < g_2 < 0.31 \leftarrow \beta \sim 0.77$
 Boosted and threshold production



Theoretical input:

$$\eta_W = 0$$

Qualitatively OK.

One can eliminate (or understand) the fake distribution by using events with different charges.

$$\frac{\pi^2}{16} \langle g_1 \rangle = 0.51$$

$$\frac{\pi^2}{16} \langle g_2 \rangle = 0.16$$

Summary

- * In the long-lived stau scenario, it is possible to perform a detailed analysis of **exclusive processes**.
- * Masses of superparticles (not the mass differences) can be measured with a good accuracy.
- * Chargino-neutralino production is a good process to **test** supersymmetry.
- * **P and CP (or T) violation** can be measured. We can learn about model parameters such as gaugino/higgsino mixing and left-right mixing.
- * Study of neutralino-pair production will also be important.