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Sequestering in models of F -term uplifting

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In collaboration with

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Plan of this talk

I. Introduction

Nonperturbative moduli stabilization & uplifting

II. 5D orbifold model

Dynamically sequestered F-term uplifting

III. Summary

I. Introduction

Nonperturbative moduli stabilization & uplifting

A systematic way for constructing
Minkowski (dS) minimum with low scale ~~SUSY~~
in 4D effective SUGRA

KKLT scenario with $\overline{D3}$



S : dilaton

T : size moduli $h^{1,1}$

U : shape moduli $h^{2,1}$

KKLT scenario with $\overline{D3}$

Giddings, Kachru & Polchinski, PRD66 (2002)

$$G_3 = F_3 + SH_3$$



Gukov, Vafa & Witten, NPB584 (2000)

$$W_{\text{flux}}(S, U) = \int_{CY} G_3 \wedge \Omega$$

$\langle S \rangle$: ~~dilaton~~

T : size moduli $h^{1,1}$

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$\langle U \rangle$: ~~shape moduli~~ $h^{2,1}$

$$\left\{ \begin{array}{l} K_0 = -3 \ln(\tau + \bar{\tau}) \\ W_0 = c \end{array} \right.$$

$$a \sim 4\pi^2$$

$$c \equiv \langle W_{flux} \rangle$$

$$M_{pl} = 1$$



Kachru, Kallosh, Linde & Trivedi, PRD68 (2003)

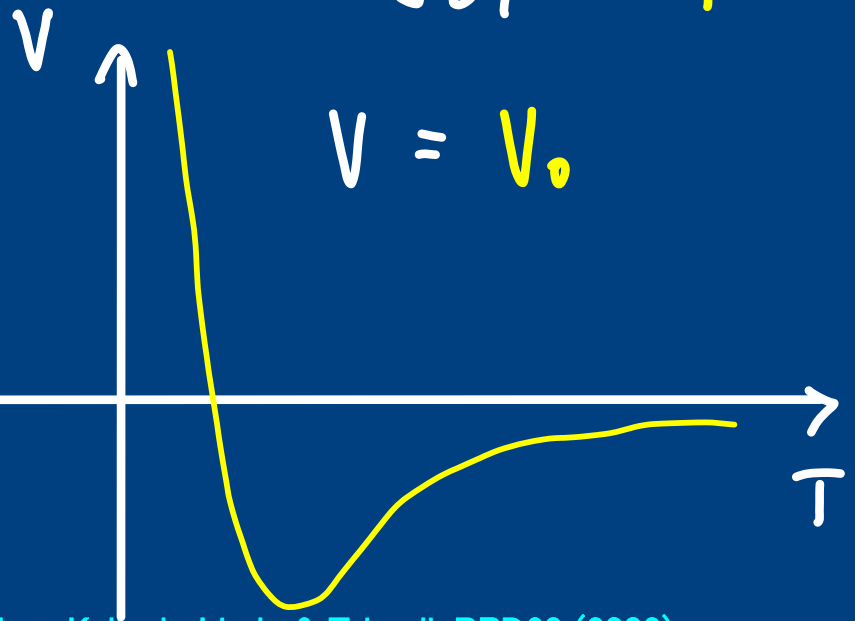
KKLT scenario with $\overline{D3}$

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$$G_3 = F_3 + SH_3$$



$$f_{D7} = T$$



$$V = V_0$$

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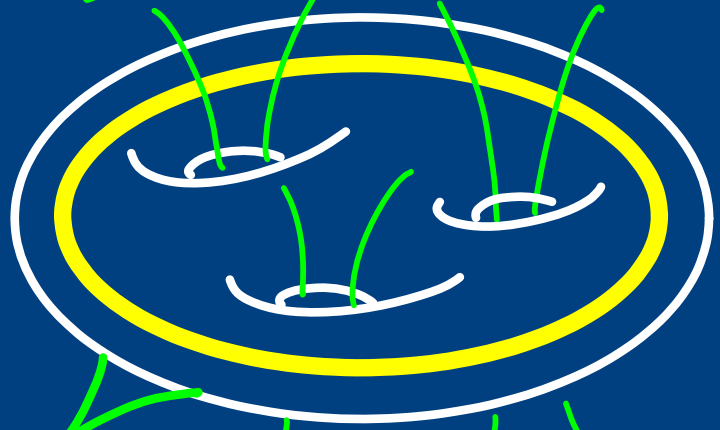
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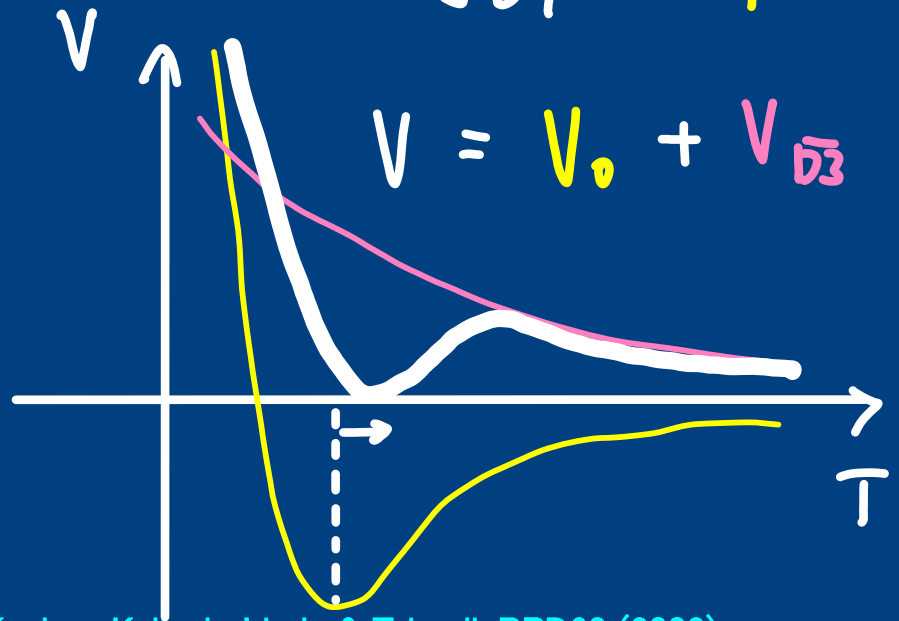
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$\overline{D3}$

$$f_{D7} = T$$

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$$V = V_0 + V_{\overline{D3}}$$

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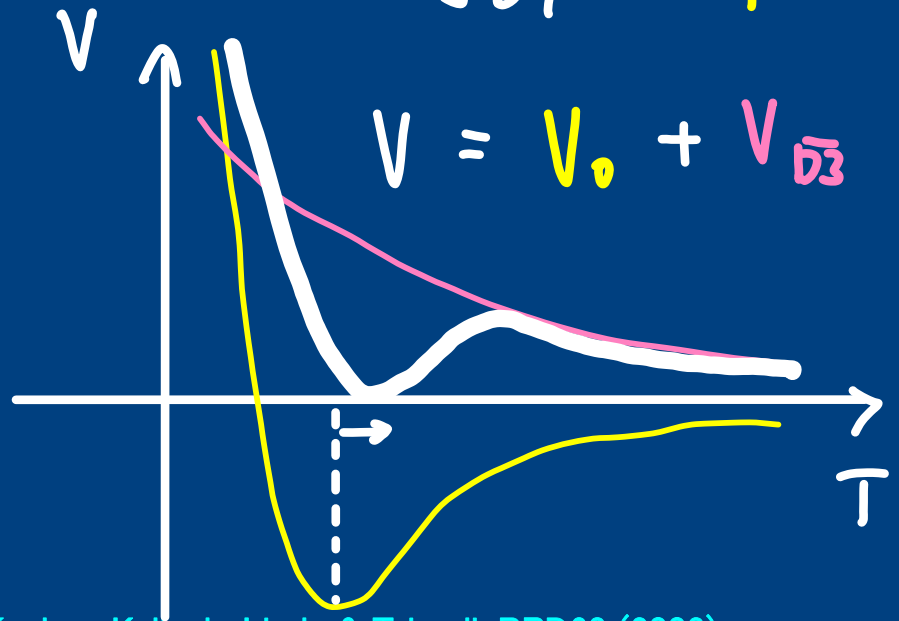
$$\begin{cases} K_0 = -3 \ln(\tau + \bar{\tau}) \\ W_0 = c - A e^{-aT} \end{cases}$$

$$a \sim 4\pi^2$$

$$m_{3/2} \simeq c \equiv 10^{-14} \quad c \equiv \langle W_{flux} \rangle$$

$$m_T \simeq a m_{3/2} \quad M_{pl} = 1$$

$$FT \simeq \frac{m_{3/2}}{\ln(M_{pl}/m_{3/2})} \sim \frac{m_{3/2}}{4\pi^2}$$



$$V = V_0 + V_{\overline{D3}}$$

Kachru, Kalosh, Linde & Trivedi, PRD68 (2003)

Choi, Falkowski, Nilles & Olechowski, NPB718 (2005)

F-term uplifting

Saltman & Silverstein, JHEP0411 (2004)

Lebedev, Nilles & Ratz, PLB636 (2006)

Gomez-Reino & Scrucca, JHEP0605 (2006)

Dudas, Papineau & Pokorski, JHEP0702 (2007),

Higaki, Kobayashi, Omura & H.A., PRD75 (2007), ...

$$V = V_0 + V_{D3}$$

Explicit ~~SUSY~~

$$\left\{ \begin{array}{l} K_0 = -3 \ln(\tau + \bar{\tau}) \\ W_0 = c - A e^{-a\tau} \end{array} \right.$$

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$$V = V_0 + \cancel{V_D}$$

Explicit ~~SUSY~~ \rightarrow Dynamical ~~SUSY~~ (DSB)

$$\left\{ \begin{array}{l} K_0 = -3 \ln(\tau + \bar{\tau}) + \sum_{X\bar{X}} (\tau, \bar{\tau}) |X|^2 \\ W_0 = c - A e^{-a\tau} + \underset{\text{Polonyi}}{f(\tau) X} \end{array} \right.$$

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Explicit ~~SUSY~~ \rightarrow Dynamical ~~SUSY~~ (DSB)

$$\left\{ \begin{array}{l} K_0 = -3 \ln(\tau + \bar{\tau}) + \sum_{X\bar{X}} (\tau, \bar{\tau}) |X|^2 \\ \quad - \frac{1}{4\pi^2 m^2} |X|^4 \leftarrow \text{integrate} \\ W_0 = c - A e^{-a\tau} + f(\tau) X + \left(\begin{array}{l} \text{heavy modes} \\ \text{with mass } m \end{array} \right) \\ \text{Polonyi, O'R, ISS, ...} \end{array} \right.$$

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For $\frac{m}{M_{\text{Pl}}} \ll 1$, $\langle X \rangle \sim m^2 \ll 1$, $F^X \sim f \approx c \sim m_{3/2}$ $M_{\text{Pl}} = 1$

DSB sector X can play a role of $\bar{D}3$ in KKLT

$$V_{\text{min}} \sim -|V_{\text{moduli}}| + |V_{\text{DSB}}| \approx 0$$

Issues of flavor in models of F-term uplifting

F-term uplifting provides a systematic way for constructing realistic vacua i.e. Minkowski (dS) min. with low scale SUSY

Next task Concrete realization of

Visible (MSSM) sector

Hidden (DSB) sector

Issues of flavor in models of F-term uplifting

F-term uplifting provides a systematic way for constructing realistic vacua i.e. Minkowski (dS) min. with low scale ~~SUSY~~

Next task Concrete realization of

Visible (MSSM) sector

Matter content
Gauge, Yukawa couplings
Soft ~~SUSY~~ terms, ...

$F^X, F^T \neq 0$

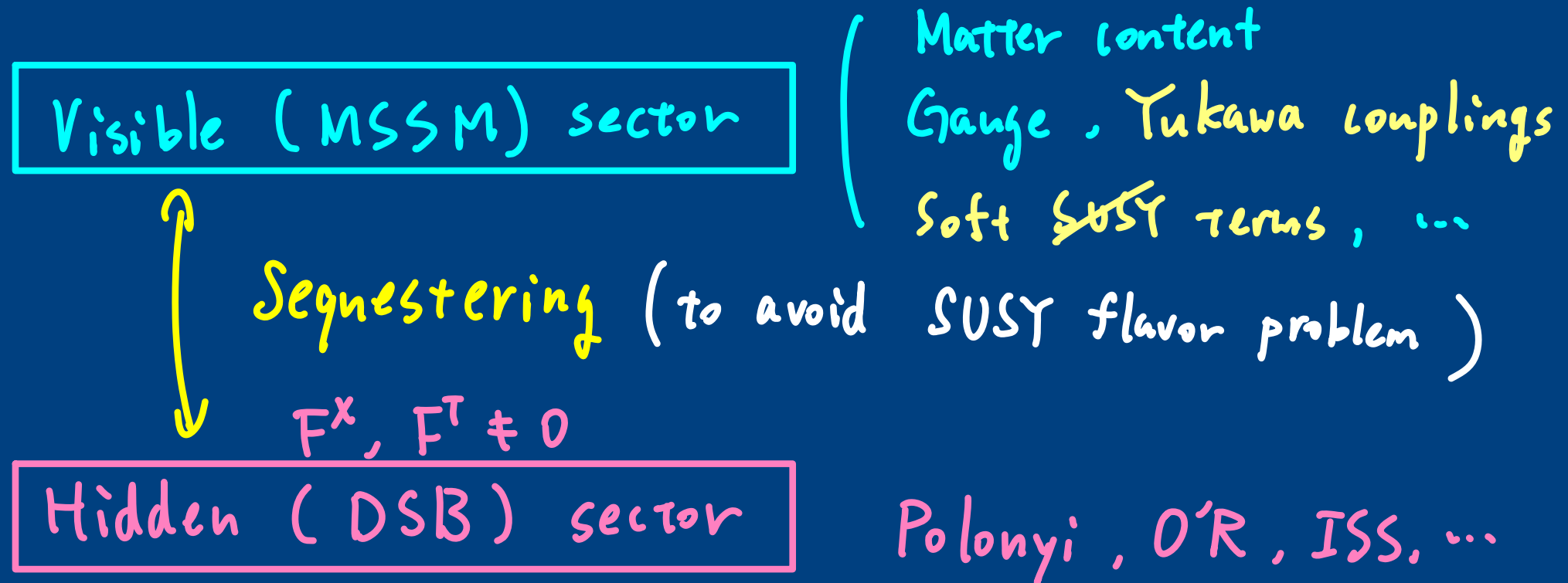
Hidden (DSB) sector

Polonyi, O'R, ISS, ...

Issues of flavor in models of F-term uplifting

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Next task Concrete realization of



→ Simplified model with SUSY, extra dim. ...

II. 5D orbifold model

Dynamically sequestered F-term uplifting

F-term uplifting in 5D orbifold model

Ex. 5D SUGRA on S^1/\mathbb{Z}_2

$X = (\text{DSB sector})$

$$Q^I = \begin{pmatrix} Q^i, U^i, D^i \\ L^i, E^i, H_u, H_d \end{pmatrix}$$

} Bulk hyper $\mathcal{H}^I = (H^I, \cancel{H_c^I})$



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Bulk hyper $\mathcal{H}^I = (H^I, \cancel{H_c^I})$

$$K_0 = -3 \ln(\tau + \bar{\tau})$$

$$+ Z_{X\bar{X}}(\tau, \bar{\tau}) |X|^2$$

$$+ Z_{I\bar{I}}(\tau, \bar{\tau}, |X|^2) |Q^I|^2$$

+ ...

$$W_0 = c - A e^{-a\tau} + f X + \lambda_{IJK} Q^I Q^J Q^K + \dots$$

F-term uplifting in 5D orbifold model

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+ ...



superpotential at fixed points

$$W_0 = \underbrace{c - A e^{-a\tau}}_{\text{NP effects from (fixed points bulk)}} + f X + \lambda_{IJK} Q^I Q^J Q^K + \dots$$

NP effects from (fixed points bulk)

F-term uplifting in 5D orbifold model

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$$+ Z_{I\bar{I}}(\tau, \bar{\tau}, |X|^2) |Q^I|^2$$

Calculable! + ...



superpotential at fixed points

$$W_0 = \underbrace{c - A e^{-a\tau}}_{\text{NP effects from (fixed points bulk)}} + f X + \lambda_{IJK} Q^I Q^J Q^K + \dots$$

NP effects from (fixed points bulk)

Yukawa hierarchy in 5D orbifold model

Ex. 5D SUGRA on S^1/Z_2

Gherghetta & Pomarol, NPB586 (2000)

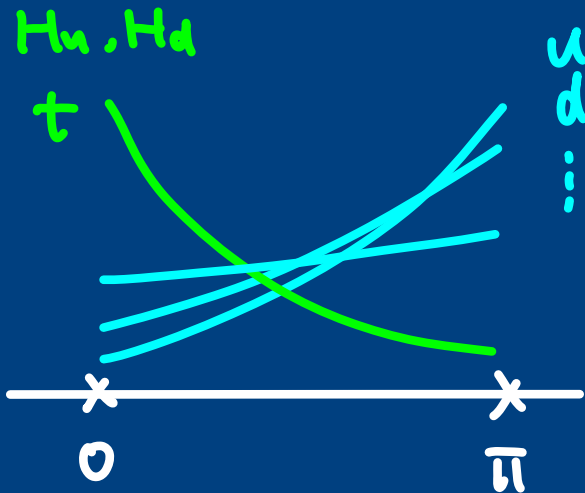
$$\chi^I \sim e^{-c_I y} Q^I + \dots \quad \text{E.O.M}$$

$c_I \sim U(1)$ charge for graviphoton

$$Z_{I\bar{J}} = e^{\frac{1}{3}k_0} \frac{1 - |e^{-c_I T}|^2}{c_I} \delta_{I\bar{J}}$$

$$\rightarrow T + \bar{T} \quad (c_I \rightarrow 0)$$

$$y_{IJK} \sim \lambda_{IJK} (e^{k_0} Z_{I\bar{I}} Z_{J\bar{J}} Z_{K\bar{K}})^{\frac{1}{2}}$$

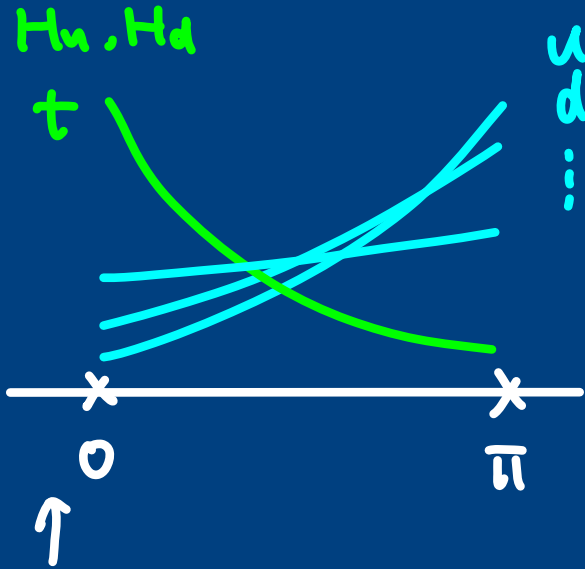


$$\lambda_{IJK} \approx 1 \quad (\forall I, J, K)$$

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$$c_g \sim (-3, -2, 2)$$

$$c_u \sim (-5, -2, 2)$$

$$c_d \sim (-3, -3, -2)$$

$$c_{H_u} = c_{H_d} \sim 2$$

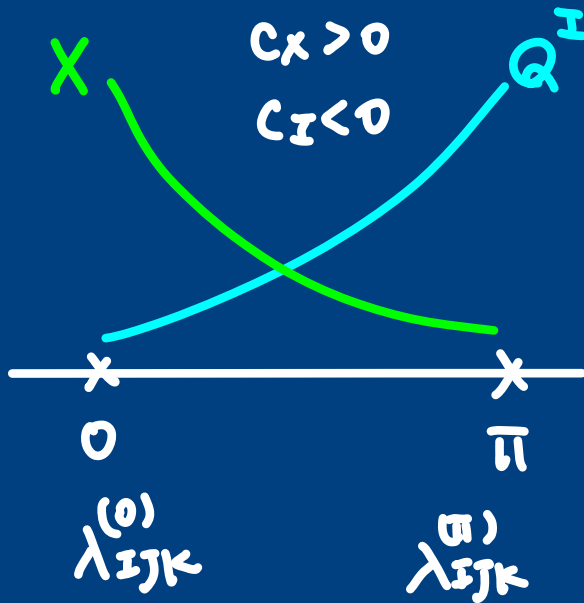
$$y_u \sim \begin{pmatrix} \epsilon^8 & \epsilon^5 & \epsilon^3 \\ \epsilon^7 & \epsilon^4 & \epsilon^2 \\ \epsilon^5 & \epsilon^2 & 1 \end{pmatrix}, \quad y_d \sim \begin{pmatrix} \epsilon^6 & \epsilon^6 & \epsilon^5 \\ \epsilon^5 & \epsilon^5 & \epsilon^4 \\ \epsilon^3 & \epsilon^3 & \epsilon^2 \end{pmatrix}$$

Choi, Kim, Kim & Kobayashi, EPJC35 (2004)

Dynamical sequestering in 5D orbifold model

Ex. 5D SUGRA on S^1/\mathbb{Z}_2

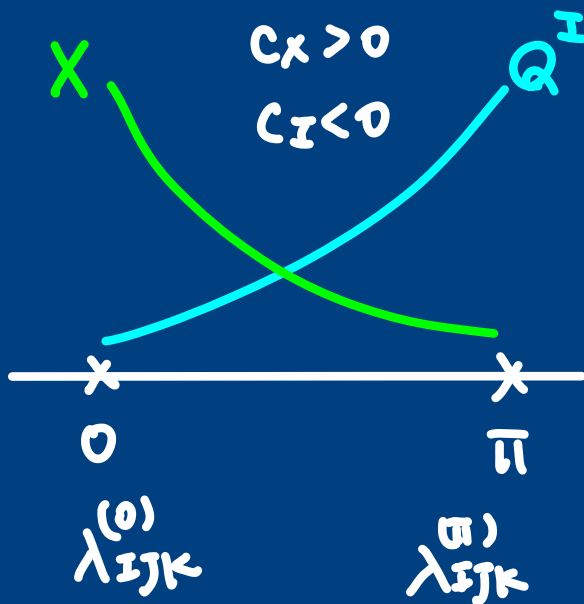
Higaki, Kobayashi, Omura & H.A., JHEP0804 (2008)



Dynamical sequestering in 5D orbifold model

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Higaki, Kobayashi, Omura & H.A., JHEP0804 (2008)



Higher order terms in K can be derived by off-shell dimensional reduction

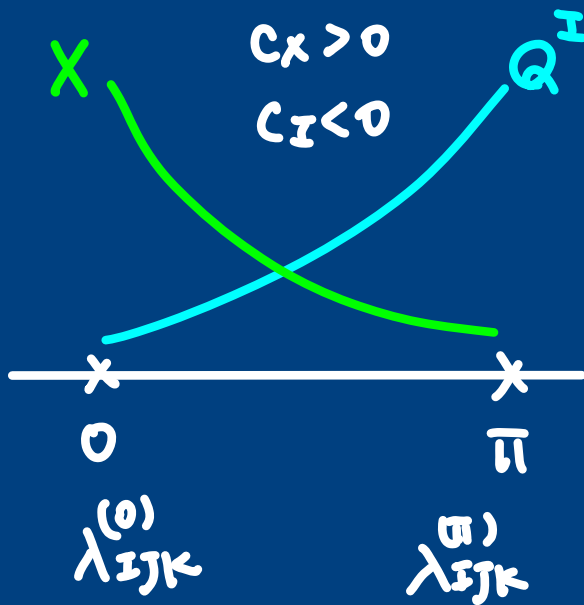
Sakamura & H.A., PRD75 (2007)

$$\begin{aligned}
 Z_{I\bar{J}} = & e^{\frac{1}{3}k_0} \frac{1 - |e^{-c_I T}|^2}{c_I} \delta_{I\bar{J}} \\
 & + \frac{1}{3} e^{\frac{1}{3}k_0} \frac{1 - |e^{-(c_I + c_x) T}|^2}{c_I + c_x} |X|^2 \delta_{I\bar{J}}
 \end{aligned}$$

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Sakamura & H.A., PRD75 (2007)

$$m_I^2 \approx \frac{c_I^2}{1 - c_I^2} \left(\frac{c_I^2}{1 - c_I^2} |F^T|^2 - \frac{1}{3} \frac{c_I^2 - c_X^2}{c_I(c_X - c_I)} |F^X|^2 \right)$$

Scalar mass

$$c_I = e^{-|c_I|T}$$

$$c_X = e^{-c_X T}$$

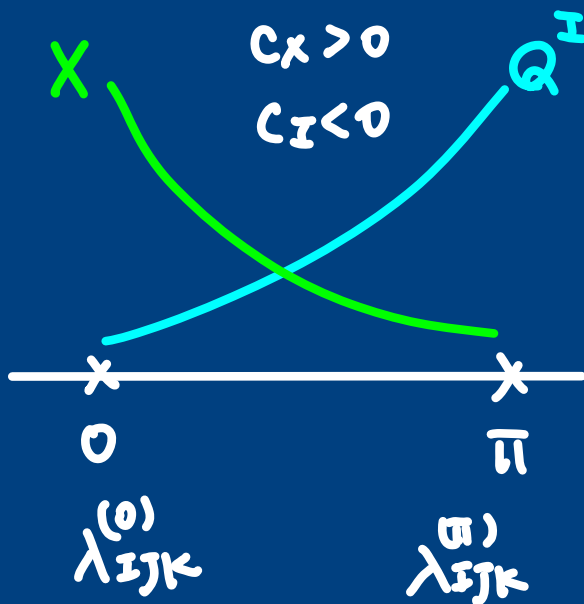
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Annotations: "Same factor" points to the circled c_I^2 terms. "Negative" points to the minus sign in the second term.

Scalar mass

$$\epsilon_I = e^{-|c_I|T}$$

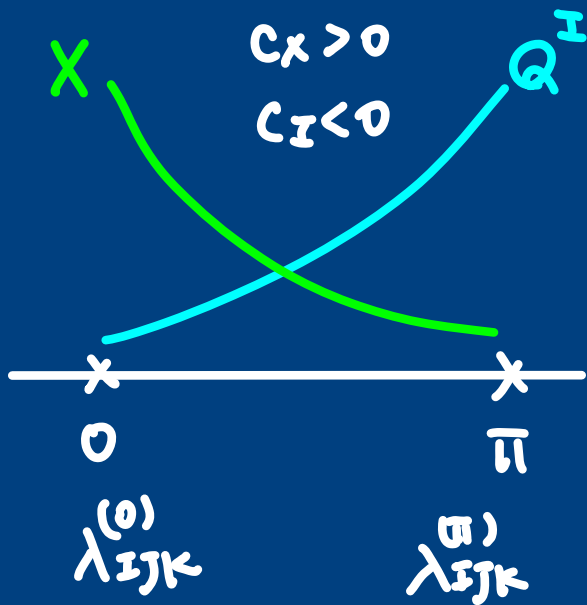
$$\epsilon_X = e^{-c_X T}$$

- ★ Modulus mediation \leq direct mediation.
- ★ Direct mediation yields tachyonic contribution.
- ★ $\epsilon_I^2, \epsilon_X \ll \frac{1}{4\pi^2} \longrightarrow$ Anomaly mediation

Dynamical sequestering in 5D orbifold model

Ex. 5D SUGRA on S^1/Z_2

Higaki, Kobayashi, Omura & H.A., JHEP0804 (2008)



Higher order terms in K can be derived by off-shell dimensional reduction

Sakamura & H.A., PRD75 (2007)

$$A_{IJK} \approx - \left\{ \left(\frac{c_I}{1 - \epsilon_I^2} + (I \leftrightarrow J) + (I \leftrightarrow K) \right) - \frac{(c_I + c_J + c_K) \lambda_{IJK}^{(\pi)}}{\lambda_{IJK}^{(0)} \epsilon_I \epsilon_J \epsilon_K + \lambda_{IJK}^{(\pi)}} \right\} F^T$$

$$+ \frac{\lambda_{IJK, X}^{(0)} \epsilon_I \epsilon_J \epsilon_K + \lambda_{IJK, X}^{(\pi)} \epsilon_X}{\lambda_{IJK}^{(0)} \epsilon_I \epsilon_J \epsilon_K + \lambda_{IJK}^{(\pi)}} F^X$$

A-term

$$\epsilon_I = e^{-|c_I|T}$$

$$\epsilon_X = e^{-c_X T}$$

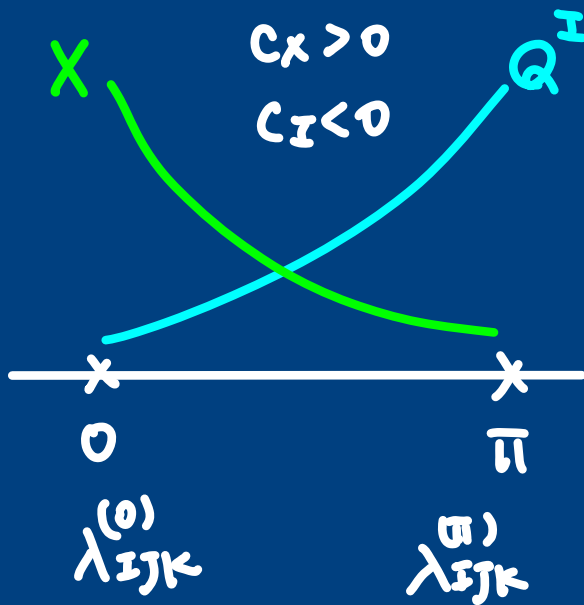
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$\epsilon_I^2 \leftarrow$

A-term

$$\epsilon_I = e^{-|c_I|T}$$

$$\epsilon_X = e^{-c_X T}$$

$$+ \frac{\lambda_{IJK, X}^{(0)} \epsilon_I \epsilon_J \epsilon_K + \lambda_{IJK, X}^{(\pi)} \epsilon_X}{\lambda_{IJK}^{(0)} \epsilon_I \epsilon_J \epsilon_K + \lambda_{IJK}^{(\pi)}} F^X$$

$\star \epsilon_I^2, \epsilon_X \ll \frac{1}{4\pi^2} \xrightarrow{\lambda_{IJK}^{(\pi)} \neq 0} \text{Anomaly mediation}$

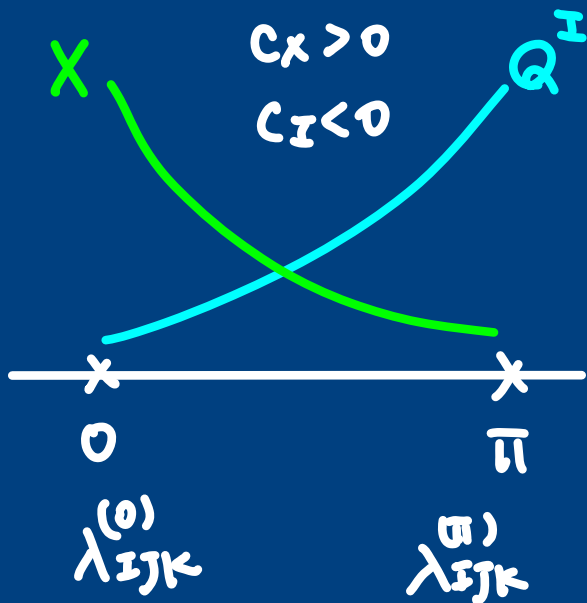
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$$A_{IJK} \approx - \left\{ \left(\frac{c_I}{1 - \epsilon_I^2} + (I \leftrightarrow J) + (I \leftrightarrow K) \right) - \frac{(c_I + c_J + c_K) \lambda_{IJK}^{(\pi)}}{\lambda_{IJK}^{(0)} \epsilon_I \epsilon_J \epsilon_K + \lambda_{IJK}^{(\pi)}} \right\} F^T$$

$\lambda_{IJK}^{(\pi)} \neq 0$
 $\lambda_{IJK}^{(0)} = 0$

$\epsilon_I^2 \leftarrow$
 $c_I + c_J + c_K \swarrow$

A-term

$$+ \frac{\lambda_{IJK, x}^{(0)} \epsilon_I \epsilon_J \epsilon_K + \lambda_{IJK, x}^{(\pi)} \epsilon_x}{\lambda_{IJK}^{(0)} \epsilon_I \epsilon_J \epsilon_K + \lambda_{IJK}^{(\pi)}} F^x$$

$$\epsilon_I = e^{-|c_I|T}$$

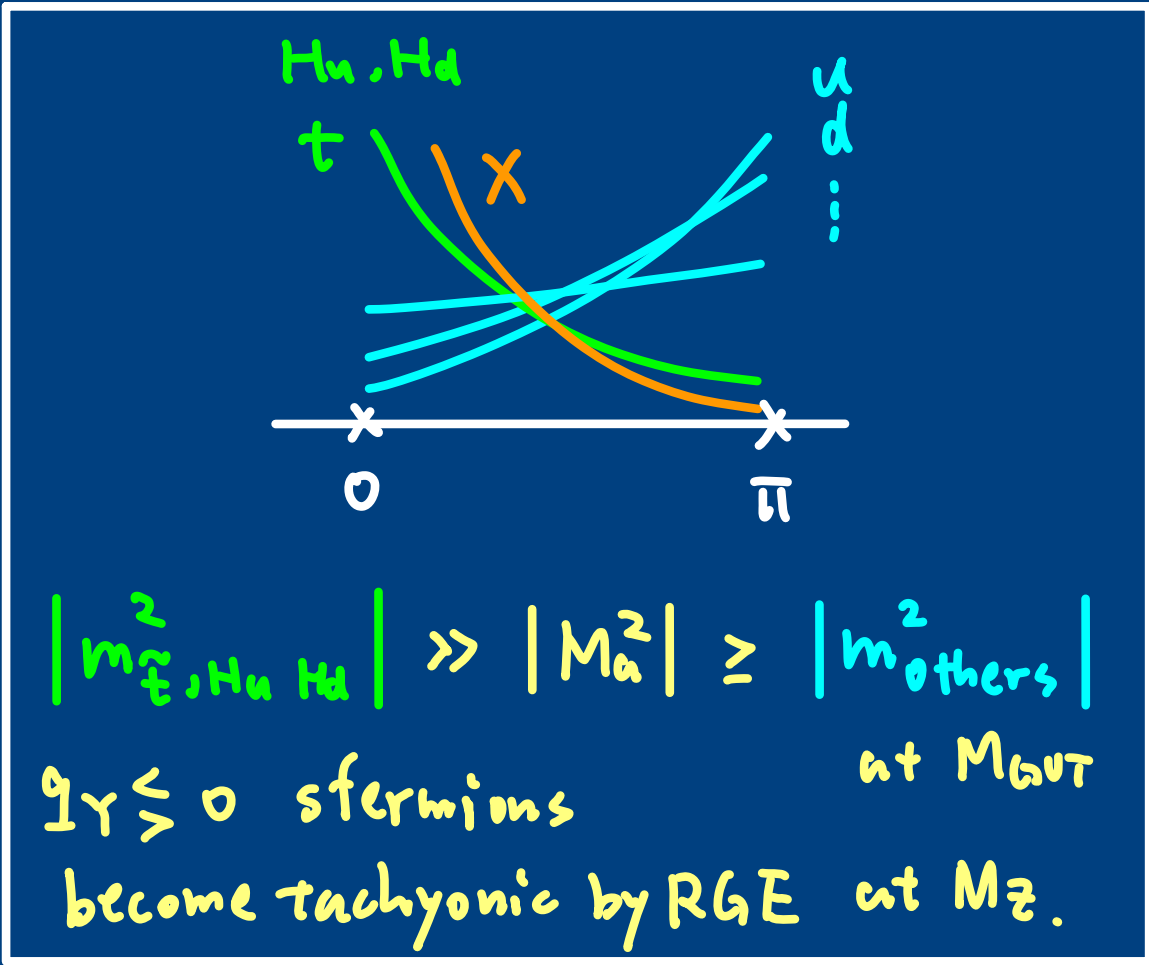
$$\epsilon_x = e^{-c_x T}$$

★ $\epsilon_I^2, \epsilon_x \ll \frac{1}{4\pi^2}$

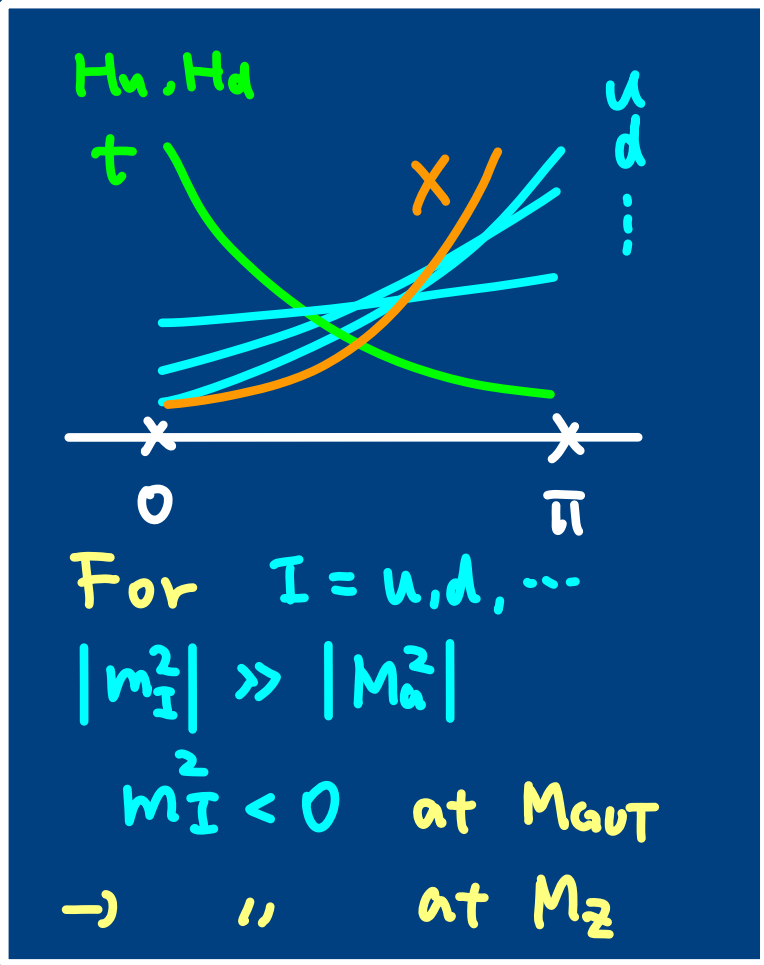
$\lambda_{IJK}^{(\pi)} \neq 0 \rightarrow$ Anomaly mediation

$\lambda_{IJK}^{(0)}, \lambda_{IJK, x}^{(0, \pi)} = 0 \rightarrow$ Modulus mediation

Yukawa hierarchy v.s. sequestering in 5D



or



Either Yukawa hierarchy or sequestering by wavefunc. localization \rightarrow
 { Multi moduli (Y. Sakamura's talk)
 6D SUGRA

III. Summary

Sequestering in models of F-term uplifting

F-term uplifting provides a systematic way for constructing realistic vacua i.e. $SUSY$ Minkowski (dS) min.

Flavor issues

★ Some implications from a simple 5D model.

- Dynamical sequestering by wave func. localization
- Either Yukawa hierarchy or sequestering

Fixed point dynamics, more than single ED (modulus) ?

★ Still challenging issue in supergravity/string models

- Extension to magnetized D-brane models

END