

Moduli stabilization with Matter uplifting
in Heterotic string theory

SUSY 08

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based on the work in progress with S. Shin

Low energy effective theory from string compactifications

Couplings = $f(\langle S \rangle, \langle T \rangle)$,

S (Dilaton) : string coupling strength

T (Volume modulus) : size of the compactified space

\Rightarrow Moduli F -terms (F^S, F^T) : source of soft SUSY breaking terms

Moduli stabilization : NP effects and fluxes are natural sources of moduli fixing.

Nearly flat dS vacuum

Supersymmetric field configuration always extremizes scalar potential V .

$$F^S = F^T = 0 \Rightarrow \langle V \rangle < 0,$$

Kachru, Kallosh, Linde, Trivedi

Uplifting effects - KKLT (type IIB) : anti-branes (non-linearly realized SUSY)

- Matter uplifting : hidden sector F -term SUSY breaking

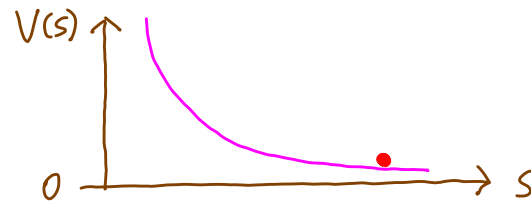
Dilaton stabilization in heterotic string

Gauge kinetic function : $f_a = S$ ($\text{Re} S_0 \approx 2$ for gauge coupling unification)

\Rightarrow Gaugino condensation would generate NP superpotential $W_{\text{NP}} \sim e^{-a_s}$.

Tree-level Kähler potential + NP superpotential with single gaugino condensate

\Rightarrow Run-away potential

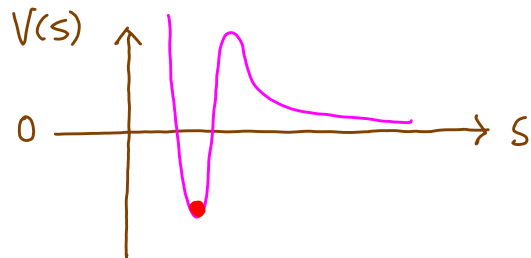


Krasnikov, Casas

(I) Race-track mechanism

(controllable) NP superpotential with multi gaugino condensates

$$W_{\text{NP}} = A_1 e^{-a_1 s} - A_2 e^{-a_2 s}, \quad (A_1, A_2 = \mathcal{O}(1), \quad a_1, a_2 = \mathcal{O}(4\pi^2))$$



\Rightarrow little fine tuning : $(a_1 - a_2) / (a_1 + a_2) \sim \frac{1}{4\pi^2}$,

Typically $F^S \sim 0$, $F^T \sim m_{3/2}$

AdS vacuum : $\langle V \rangle \sim -m_{3/2}^2 M_{\text{Pl}}^2$,

Casas, Binetruy et al, Barreiro et al,

(2) Large (uncontrollable) NP corrections to Kähler potential

Wsp : single gaugino condensate



$$\Rightarrow F^S \sim M_{3/2}, F^T = 0 \text{ (T-duality)}$$

$$dS \text{ vacuum : } \langle V \rangle \sim M_{3/2}^2 M_{pl}^2.$$

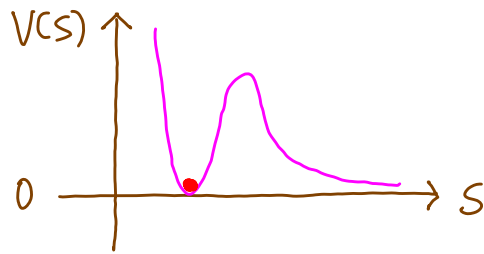
* For both (1), (2), it is difficult to tune the vacuum energy to be small enough.

Löwen, Nilles

Matter uplifting in heterotic

Löwen, Nilles: Polony type uplifting sector (Z).

Tree-level Kähler potential + Wnp with single gaugino condensate



$\Rightarrow S$ is stabilized at a dS vacuum with $\langle V \rangle \approx 0$.

Little hierarchy structure: $F^Z \sim m_{3/2}$.

$$F^S \sim m_{3/2} / \ln(M_{\text{Pl}} / m_{3/2}).$$

$f_a = S$: Dilaton mediation gives comparable contribution to gaugino masses as anomaly mediation ($\sim m_{3/2} / 8\pi^2$, always present).

\Rightarrow Mirage pattern of gaugino masses

Stabilization of volume modulus T

$\rightarrow T$ is assumed to be fixed at a self dual point (T-duality) with $F^T = 0$.

* Generically uplifting matter Z has non-trivial $SL(2, Z)$ modular transformation,

→ SUSY breaking by Z might shift T from the self dual point, if then $F^T \sim M^{3/2}$.

* In the absence of uplifting sector, the self dual points typically correspond to local maxima or saddle points.

→ Uplifting potential might give an important contribution to M_τ .

In this work,

1. We examine moduli stabilization and SUSY breaking in the L wen-Nilles scheme while explicitly including T ,

2. Generalizing the scheme to the situation with an anomalous $U(1)$ gauge symmetry, we also examine the effects of anomalous $U(1)$ sector.

(effective theories from string theory often contain anomalous $U(1)$ gauge symmetries.)

1. Moduli stabilization with matter uplifting

Modular invariant action (tree-level Kähler potential)

$$K = -\ln(S+\bar{S}) - 3\ln(T+\bar{T}) + (T+\bar{T})^n Z\bar{Z}, \quad n: \text{modular weight of } Z$$

$$W = \eta(T)^{-6} \Omega(S, T, Z), \quad \eta(T): \text{Dedekind eta function of modular weight } \frac{1}{2}$$

$$\Rightarrow G = K + \ln|W|^2 \text{ and } \Omega \text{ are modular invariant.}$$

Perturbative shift symmetry ($\text{Im}S \rightarrow \text{Im}S + \text{constant}$) $\Rightarrow \Omega \sim e^{-aS}$ (gaugino condensation)

Scalar potential

$$V_F = e^G \left(G_{I\bar{J}}^{-1} G_I G_{\bar{J}} - 3 \right), \quad G_I \equiv \partial_I G.$$

$$F\text{-term: } F^I = -e^{G/2} G_{I\bar{J}}^{-1} G_{\bar{J}}, \quad (\text{SUSY breaking})$$

Modular invariance : properties at self dual points ($T=1, e^{2\pi i/6}$)

(1) $F^T \propto G_{Z\bar{Z}}G_{T\bar{T}} - G_{T\bar{T}}G_{Z\bar{Z}} = 0$ for $\forall Z$.

\Rightarrow Fixed at a self dual point, T does not break SUSY.

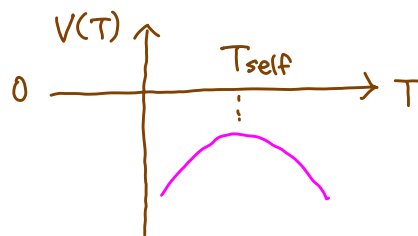
(2) For Z satisfying $nZ\partial_Z V_F = 0$, the modular invariance leads to $\partial_T V_F = 0$.

\Rightarrow self dual points are stationary points of potential ($\partial_Z V_F = 0 \Rightarrow \partial_T V_F = 0$).

Stabilization of volume modulus T

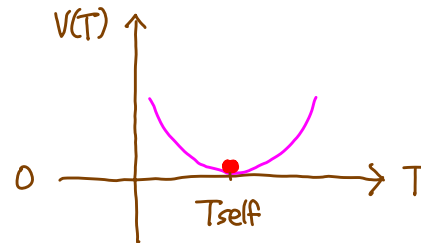
In the field basis $(S, T, Z' = \eta(T)^{-2n} Z)$, there are no mass mixings between T and (S, Z') .
(Z' : modular weight=0)
 where n (matter modular weight) is a non-positive rational number of $\mathcal{O}(1)$.

\Rightarrow For $\langle V_F \rangle \approx 0$ with reasonable values of n and Z_0 , it turns out that self dual points correspond to local minima ($m_T \sim m_{3/2}$).



(saddle or maximum)

\rightarrow
uplifting



$\Rightarrow T$ can be stabilized at a self dual point without breaking SUSY.

SUSY breaking pattern

From $\partial_z V_F = 0$, ① T can be stabilized at a self dual point with $F^T = 0$,

$$\textcircled{2} \text{ for } V_F = 0, \quad G_{SZ} F^S + G_{ZZ} F^Z + G_{Z\bar{Z}} F^{Z*} = 0.$$

NP origin of dilaton superpotential : it is natural possibility to have $(S = \mathcal{O}(1))$ $|G_{SZ}| \gg |G_{ZZ}|, |G_{Z\bar{Z}}|$,

→ F^S is then suppressed compared to F^Z ,

→ F^Z is the main source of SUSY breaking ($V_F = 0$).

Löwen, Nilles : $W = A e^{-\alpha S} + \omega + \mu^2 Z$ (Polony-type superpotential for Z)

⇒ S and Z are well stabilized at a dS vacuum with $\langle V_F \rangle \approx 0$,

$$F^S \sim F^Z / \ln(M_{\text{pl}} / m_{3/2}), \quad M_S \sim \ln(M_{\text{pl}} / m_{3/2}) m_{3/2}, \quad m_Z \sim m_{3/2}.$$

The uplifting sector plays a crucial role both in stabilizing S and in adjusting the vacuum energy.

2. Moduli stabilization in the presence of anomalous U(1)

String compactification often involves an anomalous U(1) gauge symmetry with anomalies cancelled by Green-Schwarz mechanism:

$$f_a = S,$$

$$\text{U(1) transformation: } S \rightarrow S - i\alpha_A(x) \cdot \delta_{GS}, \quad \delta_{GS} = \mathcal{O}(1/8\pi^2)$$

$$\Rightarrow \text{Field-dependent FI term: } \sum_{\text{FI}} = \delta_{GS} \partial_s K = \mathcal{O}(M_{\text{Pl}}^2/8\pi^2) \quad \text{for } S = \mathcal{O}(1).$$

U(1) charged field X to avoid a large FI D-term

$$D_A \sim \sum_{\text{FI}} + g_X |X|^2 \approx 0 \Rightarrow \langle X \rangle \sim \sqrt{\sum_{\text{FI}}} : \text{spontaneous breaking of U(1)}$$

- Massive vector superfield $\sim V_A + g_X \ln|X|$ (Goldstone: composed mostly of X)
- Flat direction of D-term potential $\sim S$ (need to stabilize S)
- Gauge boson mass: $M_A^2 = \mathcal{O}(\delta_{GS} M_{\text{Pl}}^2)$

Effects of U(1)

Gauge invariance + stationary conditions

→ relation between VEVs of U(1) charged F-terms and D-term

For $V_{\text{tot}} = V_F + V_D \approx 0$ with $m_{3/2} \ll M_{\text{pl}}$, and $S = \mathcal{O}(1)$

$$F^S \sim g_X \frac{F^X}{X_0}, \quad D_A \sim g_X \left| \frac{F^X}{X_0} \right|^2$$

⇒ (1) D-term contribution to vacuum energy

$$V_{\text{tot}} = |D_A|^2 + |F|^2 - 3 m_{3/2}^2 M_{\text{pl}}^2 : \text{negligible compared to F-term contributions}$$

(2) D-term contribution to sfermion masses

$$m_i^2 = -g_i D_A : \text{comparable to the dilaton mediation}$$

(D-term SUSY breaking induces only soft scalar masses)

SOFT SUSY breaking terms

$$(F^T = 0)$$

Source of soft terms: Dilaton mediation $F^S \sim m_{3/2} / \ln(M_{Pl}/m_{3/2})$

Uplifting sector mediation $F^Z \sim m_{3/2}$

U(1)A sector mediation $\frac{F^X}{X_0} \sim F^S, D_A \sim |F^S|^2$

Anomaly mediation $\sim m_{3/2} / 8\pi^2$

Pattern of soft terms: dependence of effective couplings on S, Z, X, V_A

$$\mathcal{L} = \int d^4\theta \gamma_i \bar{Q}^i e^{2\delta_i V_A} Q^i + \left\{ \int d^2\theta \left(\frac{1}{4} f_a W^a W^a + \lambda_{ijk} Q^i Q^j Q^k \right) + \text{h.c.} \right\}$$

$f_a = S$ (tree-level)

(perturbative shift symmetry, $\text{Im} S$)

$$\gamma_i = (S + \bar{S})^{\frac{1}{3}} \cdot \left(1 + \underbrace{\sum_j \left| \frac{Z_j}{M_{Pl}} \right|^2}_{\text{wavy}} + \underbrace{\eta_i \left| \frac{X}{M_{Pl}} \right|^2}_{\text{wavy}} \right), \quad \lambda_{ijk} \propto \left(\frac{X}{M_{Pl}} \right)^{-(\delta_i + \delta_j + \delta_k) / \delta_X}$$

Effective cross-couplings with visible matter fields (source of flavor violations)

Sequestering \Rightarrow strong suppression of cross-couplings

(1) Gaugino masses at M_{GUT}

$$M_a(M_{\text{GUT}}) \quad * \text{ Dilaton mediation} = \frac{FS}{S+S^*} \sim \frac{m_{3/2}}{\ln(M_{\text{Pl}}/m_{3/2})} \quad : \text{universal}$$

* Anomaly mediation (super-conformal anomaly)

$$= \frac{ba}{16\pi^2} m_{3/2} \quad : \text{proportional to } \beta\text{-function}$$

* Uplifting sector mediation (due to the Konishi anomaly)

$$= C_a^i \tilde{\beta}_i \frac{Z_0}{M_{\text{Pl}}} \cdot \frac{1}{8\pi^2} m_{3/2} \quad : \text{non-universal (} C_a^i : \text{quadratic Casimir of } Q^i \text{)}$$

\Rightarrow negligible if $|Z_0| \ll M_{\text{Pl}}$ or $|\tilde{\beta}_i| \ll 1$ (sequestering).

(contribution from F^X : negligible because $|X_0| \ll M_{\text{Pl}}$)

Dilaton mediation gives a comparable contribution to M_a as anomaly mediation,

\Rightarrow Mirage mediation pattern (for $|Z_0| \ll M_{\text{Pl}}$ or $|\tilde{\beta}_i| \ll 1$)

(2) sfermion soft terms : $m_{\tilde{Q}}^2 |\tilde{Q}^i|^2 + A_{\tilde{Y}JK} y_{\tilde{Y}JK} \tilde{Q}^i \tilde{Q}^{\tilde{J}} \tilde{Q}^K$

$$A_{\tilde{Y}JK}(M_{\text{GUT}}) = \left[\underbrace{\left(\frac{1}{3} - \frac{g_{\tilde{X}}^i}{g_X} \right)}_{\text{red}} \underbrace{\frac{m_{3/2}}{\ln(M_{\text{Pl}}/m_{3/2})}}_{\text{blue}} - \underbrace{\gamma_{\tilde{X}}}_{\text{yellow}} \underbrace{\frac{z_0}{M_{\text{Pl}}}}_{\text{grey}} \cdot m_{3/2} \right] + [i \leftrightarrow j] + [i \leftrightarrow k],$$

$$m_{\tilde{Q}}^2(M_{\text{GUT}}) = \underbrace{\left(\frac{1}{3} - \frac{g_{\tilde{X}}^i}{g_X} \right)}_{\text{red}} \underbrace{\left| \frac{m_{3/2}}{\ln(M_{\text{Pl}}/m_{3/2})} \right|^2}_{\text{blue}} - \underbrace{\frac{d\gamma_{\tilde{X}}}{d \ln \mu}}_{\text{yellow}} \underbrace{\frac{|m_{3/2}|^2}{32\pi^2}}_{\text{yellow}} - \underbrace{\sum_i |z_0|^2}_{\text{grey}} + (\text{mixed contributions}).$$

■ Dilaton mediation : flavor-independent

■ U(1)_A sector mediation : A-couplings from F^X , sfermion masses from DA

■ Anomaly mediation : determined by the anomalous dimension of matter fields

⇒ those mediations give comparable contributions to sfermion soft terms

■ Uplifting sector mediation : $\sum_i z_i = \mathcal{O}(1)$ leads to heavy sfermion mass of $\mathcal{O}(m_{3/2})$.
(general feature of matter uplifting scenarios)

* It is plausible to assume that $g_{\tilde{X}}^i + g_{\tilde{X}}^j + g_{\tilde{X}}^k = 0$ for a large Yukawa coupling $y_{\tilde{Y}JK} = \mathcal{O}(1)$.

⇒ For $|\sum_i z_i| \ll 1$ (sequestering), sfermion soft terms take the mirage mediation pattern.

Summary

In heterotic string theory, by introducing the uplifting sector, dilaton can be stabilized at a dS vacuum with nearly vanishing vacuum energy in a controllable approximation,

* Volume modulus can be stabilized at a self dual point without breaking SUSY.

* The uplifting sector plays a crucial role in stabilizing both dilaton and volume modulus.

Within the L6wen-Nilles scheme, gaugino masses take the mirage pattern.

* In the presence of anomalous $U(1)$ gauge symmetry, $U(1)_A$ sector mediation gives a comparable contribution to sfermion soft terms as dilaton mediation.

* If visible matter fields are sequestered from the uplifting sector, sfermion soft terms also take the mirage pattern.

Note)

$$SL(2, \mathbb{Z}) : T \rightarrow \frac{aT - ib}{icT + d} \quad \text{where } ad - bc = 1 \quad (a, b, c, d \in \mathbb{Z})$$

$$\eta(\tau) \rightarrow e^{i\theta} (ic\tau + d)^{\frac{1}{2}} \eta(\tau), \quad \eta(\tau) = e^{-\frac{\pi}{12}\tau} \prod_{n=1}^{\infty} (1 - e^{-2n\pi\tau}),$$

$$\eta\left(\frac{1}{\tau}\right) = \sqrt{\tau} \eta(\tau) \quad \text{and} \quad \eta(\tau - i) = e^{i\pi/12} \eta(\tau).$$

$$\text{self dual : } T=1 \quad \text{for } T \rightarrow \frac{1}{T}, \quad (z \rightarrow \frac{z}{T})$$

$$T = e^{i\pi/6} \quad \text{for } T \rightarrow \frac{1}{T - i}$$

(fundamental domain : $\text{Re } T > 0, -\frac{1}{2} < \text{Im } T < \frac{1}{2}, |z| \leq 1$).

* T-duality, discrete shift symmetry ($T \rightarrow T + in, n \in \mathbb{Z}$),

$$|DA| \lesssim \frac{M_{3/2}^2 M_{pl}^2}{M_A^2}$$