

Signals for doubly charged Higgsinos at colliders

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Outline

- ★ *Left-Right Supersymmetry*
- ★ *Higgs Sector and Doubly Charged States*
- ★ *Extended “ino” spectrum*
- ★ *Production & Decay of doubly charged Higgsinos*
- ★ *Collider Signals*
- ★ *Conclusions & Outlook*

Supersymmetry

- ★ *Supersymmetry is by far the most popular option for beyond standard model physics.*
 - *solves the gauge hierarchy problem*
 - *candidate for cold dark matter and new (s)particles*
 - *gauge coupling unification*
- ★ *Neutrino mass generation in its minimal version*
 - *R-parity violation* $(-1)^{3(B-L)+2S}$
 - *Right-handed neutrinos (seesaw)*
- ★ *No unique supersymmetric field theory to model new physics at the TeV scale.*

Left-Right Supersymmetry

- ★ *Supersymmetric left-right theories (LRSUSY) are based on the product group:*

$$SU(3)_C \times SU(2)_L \times SU(2)_R \times U(1)_{B-L}$$

- ★ *Gauged $U(1)_{B-L}$: R -parity conserving*
- ★ *This product group is broken to $SU(3)_C \times U(1)_{em}$ by giving vevs to fields in the Higgs sector.*

$$SU(2)_R \times U(1)_{B-L} \longrightarrow U(1)_Y$$

- ★ *Neutrino masses are induced by the see-saw mechanism*

-- Higgs triplet fields with $B-L = \pm 2$

Higgs sector

- ★ The left-right symmetry is broken at a scale $\langle \Delta_R^0 \rangle = v_R$
- ★ The bi-doublet Higgs fields break the $SU(2)_L \times U(1)_Y$
- ★ Supersymmetry requires other Higgs multiplets to cancel chiral anomalies among the fermionic partners

$$\begin{aligned} \Phi_1 &= \begin{pmatrix} \Phi_{11}^0 & \Phi_{11}^+ \\ \Phi_{12}^- & \Phi_{12}^0 \end{pmatrix} \sim (1, 2, 2, 0), & \Phi_2 &= \begin{pmatrix} \Phi_{21}^0 & \Phi_{21}^+ \\ \Phi_{22}^- & \Phi_{22}^0 \end{pmatrix} \sim (1, 2, 2, 0) \\ \Delta_L &= \begin{pmatrix} \frac{1}{\sqrt{2}}\Delta_L^- & \Delta_L^0 \\ \Delta_L^{--} & -\frac{1}{\sqrt{2}}\Delta_L^- \end{pmatrix} \sim (1, 3, 1, -2), & \delta_L &= \begin{pmatrix} \frac{1}{\sqrt{2}}\delta_L^+ & \delta_L^{++} \\ \delta_L^0 & -\frac{1}{\sqrt{2}}\delta_L^+ \end{pmatrix} \sim (1, 3, 1, 2), \\ \Delta_R &= \begin{pmatrix} \frac{1}{\sqrt{2}}\Delta_R^- & \Delta_R^0 \\ \Delta_R^{--} & -\frac{1}{\sqrt{2}}\Delta_R^- \end{pmatrix} \sim (1, 1, 3, -2), & \delta_R &= \begin{pmatrix} \frac{1}{\sqrt{2}}\delta_R^+ & \delta_R^{++} \\ \delta_R^0 & -\frac{1}{\sqrt{2}}\delta_R^+ \end{pmatrix} \sim (1, 1, 3, 2) \end{aligned}$$

★ The matter fields:

$$Q = \begin{pmatrix} u \\ d \end{pmatrix} \sim \left(3, 2, 1, \frac{1}{3}\right), \quad Q^c = \begin{pmatrix} d^c \\ u^c \end{pmatrix} \sim \left(3^*, 1, 2, -\frac{1}{3}\right),$$

$$L = \begin{pmatrix} \nu \\ e \end{pmatrix} \sim (1, 2, 1, -1), \quad L^c = \begin{pmatrix} e^c \\ \nu^c \end{pmatrix} \sim (1, 1, 2, 1),$$

★ *The most general superpotential one can write is*

$$W = \mathbf{Y}_Q^{(i)} Q^T \Phi_i i\tau_2 Q^c + \mathbf{Y}_L^{(i)} L^T \Phi_i i\tau_2 L^c + i(\mathbf{h}_l L^T \tau_2 \delta_L L + \mathbf{h}_l L^{cT} \tau_2 \Delta_R L^c) \\ + \mu_3 [Tr(\Delta_L \delta_L + \Delta_R \delta_R)] + \mu_{ij} Tr(i\tau_2 \Phi_i^T i\tau_2 \Phi_j) + W_{NR}$$

and the soft terms as

$$\mathcal{L}_{soft} = [\mathbf{A}_Q^i \mathbf{Y}_Q^{(i)} \tilde{Q}^T \Phi_i i\tau_2 \tilde{Q}^c + \mathbf{A}_L^i \mathbf{Y}_L^{(i)} \tilde{L}^T \Phi_i i\tau_2 \tilde{L}^c + i\mathbf{A}_{LR} \mathbf{h}_l (\tilde{L}^T \tau_2 \delta_L \tilde{L} + \tilde{L}^{cT} \tau_2 \Delta_R \tilde{L}^c) \\ + m_\Phi^{(ij)2} \Phi_i^\dagger \Phi_j] + [(m_L^2)_{ij} \tilde{l}_{Li}^\dagger \tilde{l}_{Lj} + (m_R^2)_{ij} \tilde{l}_{Ri}^\dagger \tilde{l}_{Rj}] - M_{LR}^2 [Tr(\Delta_R \delta_R) + Tr(\Delta_L \delta_L) + h.c.] \\ - [B\mu_{ij} \Phi_i \Phi_j + h.c.]$$

- ★ *The vevs to the different scalar multiplets contributing to the symmetry breaking down to $U(1)_{em}$*

$$\langle \delta_L \rangle = \begin{pmatrix} 0 & 0 \\ v_{\delta_L} & 0 \end{pmatrix}, \quad \langle \Delta_R \rangle = \begin{pmatrix} 0 & v_{\Delta_R} \\ 0 & 0 \end{pmatrix}, \quad \langle \delta_R \rangle = \begin{pmatrix} 0 & 0 \\ v_{\delta_R} & 0 \end{pmatrix}.$$

$$\langle \Phi_1 \rangle = \begin{pmatrix} \kappa_1 & 0 \\ 0 & \kappa'_1 e^{i\omega_1} \end{pmatrix}, \quad \langle \Phi_2 \rangle = \begin{pmatrix} \kappa'_2 e^{i\omega_2} & 0 \\ 0 & \kappa_2 \end{pmatrix}, \quad \langle \Delta_L \rangle = \begin{pmatrix} 0 & v_{\Delta_L} \\ 0 & 0 \end{pmatrix},$$

Extended “ino” spectrum

Due to the extended Higgs sector, the spectrum has additional higgsinos, both neutral, singly charged and doubly charged.

$$\Delta_L^{++}, \Delta_R^{++}, \delta_L^{++}, \delta_R^{++}$$

Mass term: $\mathcal{L}_{\tilde{\Delta}} = -M_{\tilde{\Delta}--}\tilde{\Delta}_L^{--}\tilde{\delta}_L^{++} - M_{\tilde{\Delta}--}\tilde{\Delta}_R^{--}\tilde{\delta}_R^{++} + h.c.,$

where $M_{\tilde{\Delta}--} = \mu_3.$

6 charginos: $\tilde{\lambda}_L, \tilde{\lambda}_R, \tilde{\phi}_2, \tilde{\phi}_1, \tilde{\Delta}_L^{\pm}, \text{ and } \tilde{\Delta}_R^{\pm}.$

11 neutralinos: $\tilde{\lambda}_Z, \tilde{\lambda}_{Z'}, \tilde{\lambda}_{B-L}, \tilde{\phi}_{21}^0, \tilde{\phi}_{22}^0, \tilde{\phi}_{11}^0, \tilde{\phi}_{12}^0, \tilde{\Delta}_L^0, \tilde{\Delta}_R^0, \tilde{\delta}_L^0, \text{ and } \tilde{\delta}_R^0.$

Extended “ino” spectrum

For the charginos we have

$$\mathcal{L}_C = -\frac{1}{2}(\psi^{+T}, \psi^{-T}) \begin{pmatrix} 0 & X^T \\ X & 0 \end{pmatrix} \begin{pmatrix} \psi^+ \\ \psi^- \end{pmatrix} + \text{h.c.}$$

with

$$\psi^{+T} = (-i\lambda_L^+, -i\lambda_R^+, \tilde{\phi}_{1d}^+, \tilde{\phi}_{1u}^+, \tilde{\delta}_L^+, \tilde{\delta}_R^+) \quad \psi^{-T} = (-i\lambda_L^-, -i\lambda_R^-, \tilde{\phi}_{2d}^-, \tilde{\phi}_{2u}^-, \tilde{\Delta}_L^-, \tilde{\Delta}_R^-)$$

the mass eigenstates are given by

$$\tilde{\chi}_i^+ = V_{ij}\psi_j^+, \quad \tilde{\chi}_i^- = U_{ij}\psi_j^- \quad (i, j = 1, \dots, 6)$$

$$U^* X V^{-1} = M_D$$

Extended “neutralino” spectrum

$$\mathcal{L}_N = -\frac{1}{2}\psi^{0T} Z \psi^0 + \text{h.c.}$$

with

$$\psi^0 = (-i\lambda_L^0, -i\lambda_R^0, -i\lambda_{B-L}, \tilde{\phi}_{22}^0, \tilde{\phi}_{11}^0, \tilde{\Delta}_L^0, \tilde{\delta}_L^0, \tilde{\Delta}_R^0, \tilde{\delta}_R^0, \tilde{\phi}_{21}^0, \tilde{\phi}_{12}^0)^T$$

and the mass eigenstates in this case are given by

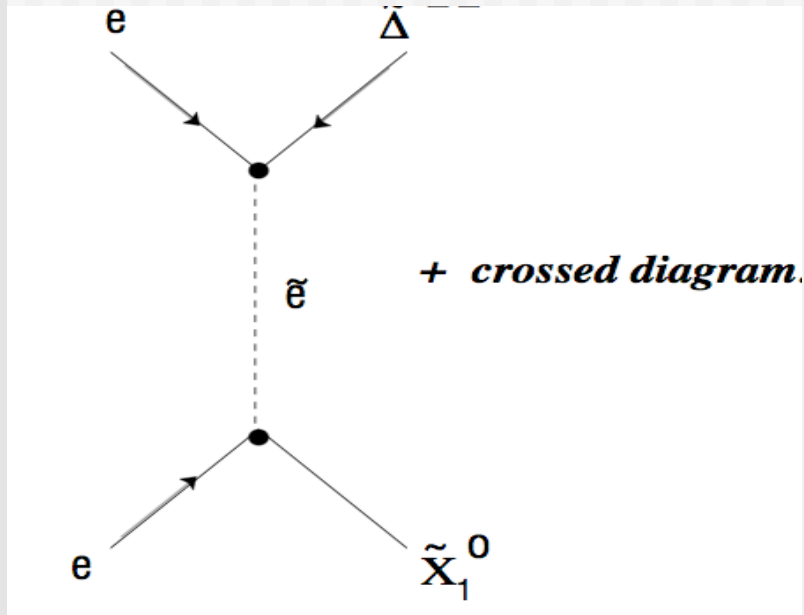
$$\tilde{\chi}_i^0 = N_{ij}\psi_j^0 \quad (i, j = 1, 2, \dots, 11)$$

The mixing matrix is diagonalised by the unitary matrix

$$N^* Z N^T = Z_D,$$

Collider Signals

Single production mode at linear $e^- e^-$ colliders



$$e^- e^- \longrightarrow \tilde{\Delta}^{--} \tilde{\chi}_1^0$$

ideal for production of such doubly charged exotics

allows to probe a large range of masses of the doubly charged Higgsinos

(pair production at $e^+ e^-$ and $\gamma\gamma$)

M. Frank, K. Huitu, SKR

Single and pair production at LHC

- $pp \longrightarrow \tilde{\chi}_1^+ \tilde{\Delta}^{--}$

- $pp \longrightarrow \tilde{\Delta}^{++} \tilde{\Delta}^{--}$

Decay modes

2-body decays

(S2)

- $\tilde{\Delta}^{--} \longrightarrow \tilde{\ell}^- \ell^-$,
- $\tilde{\Delta}^{--} \longrightarrow \Delta^{--} \tilde{\chi}_i^0$,
- $\tilde{\Delta}^{--} \longrightarrow \tilde{\chi}_i^- \Delta^-$,
- $\tilde{\Delta}^{--} \longrightarrow \tilde{\chi}_i^- W^-$,

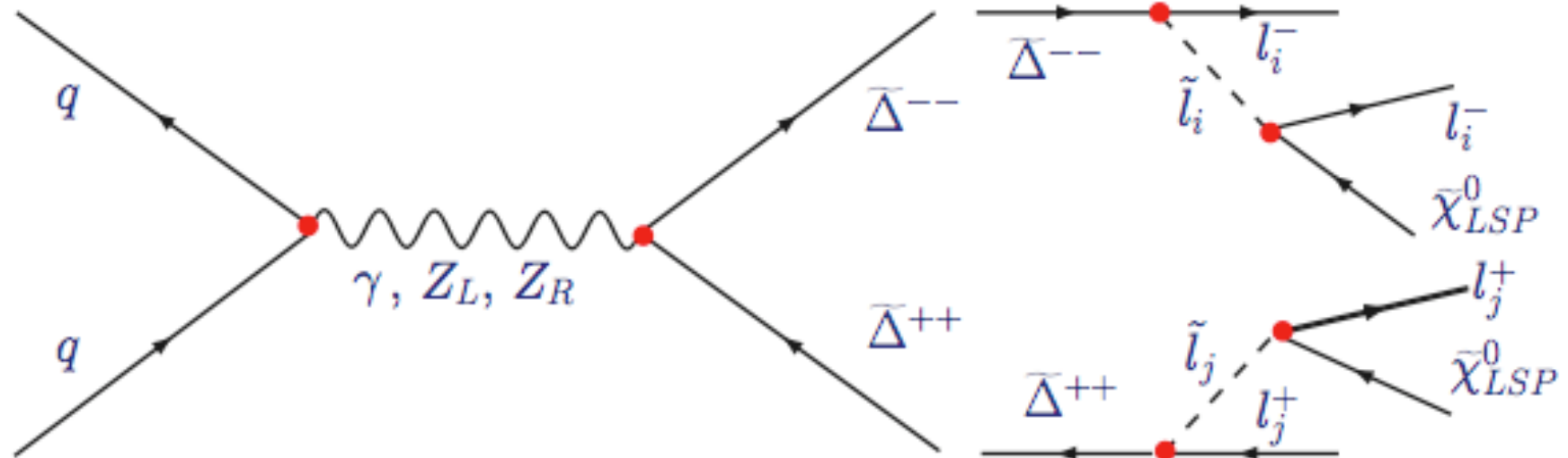
• favored channel for decay which is $\tilde{\Delta}^{--} \longrightarrow \tilde{\ell}^- \ell^-$, provided $m_{\tilde{\ell}} < M_{\tilde{\Delta}^{--}}$.

or

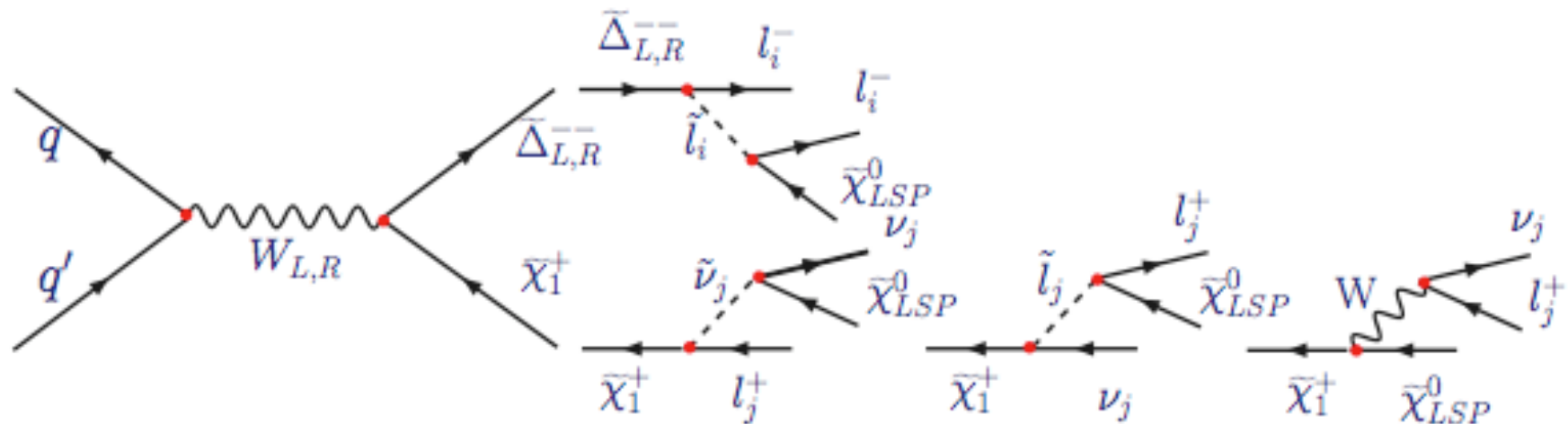
$$\tilde{\Delta}^{--} \rightarrow \tilde{\ell}^{*-} \ell^- \rightarrow \ell^- \ell^- \tilde{\chi}_1^0.$$

(S3)

4 lepton signals:



3 lepton signals:



Representative points

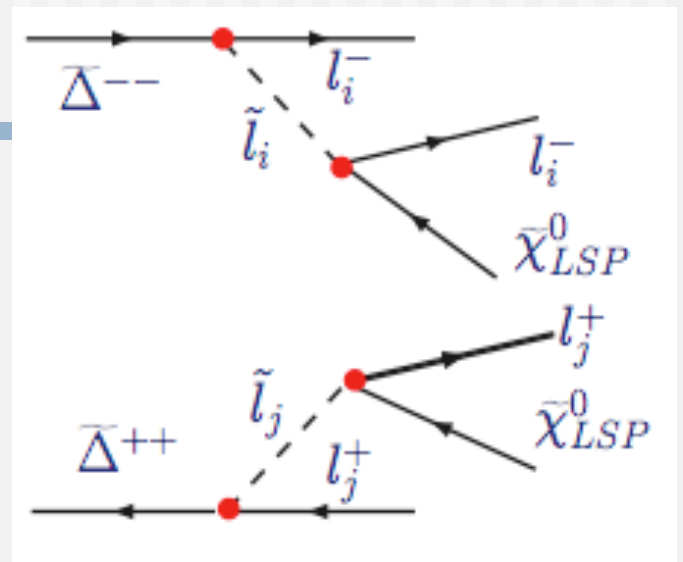
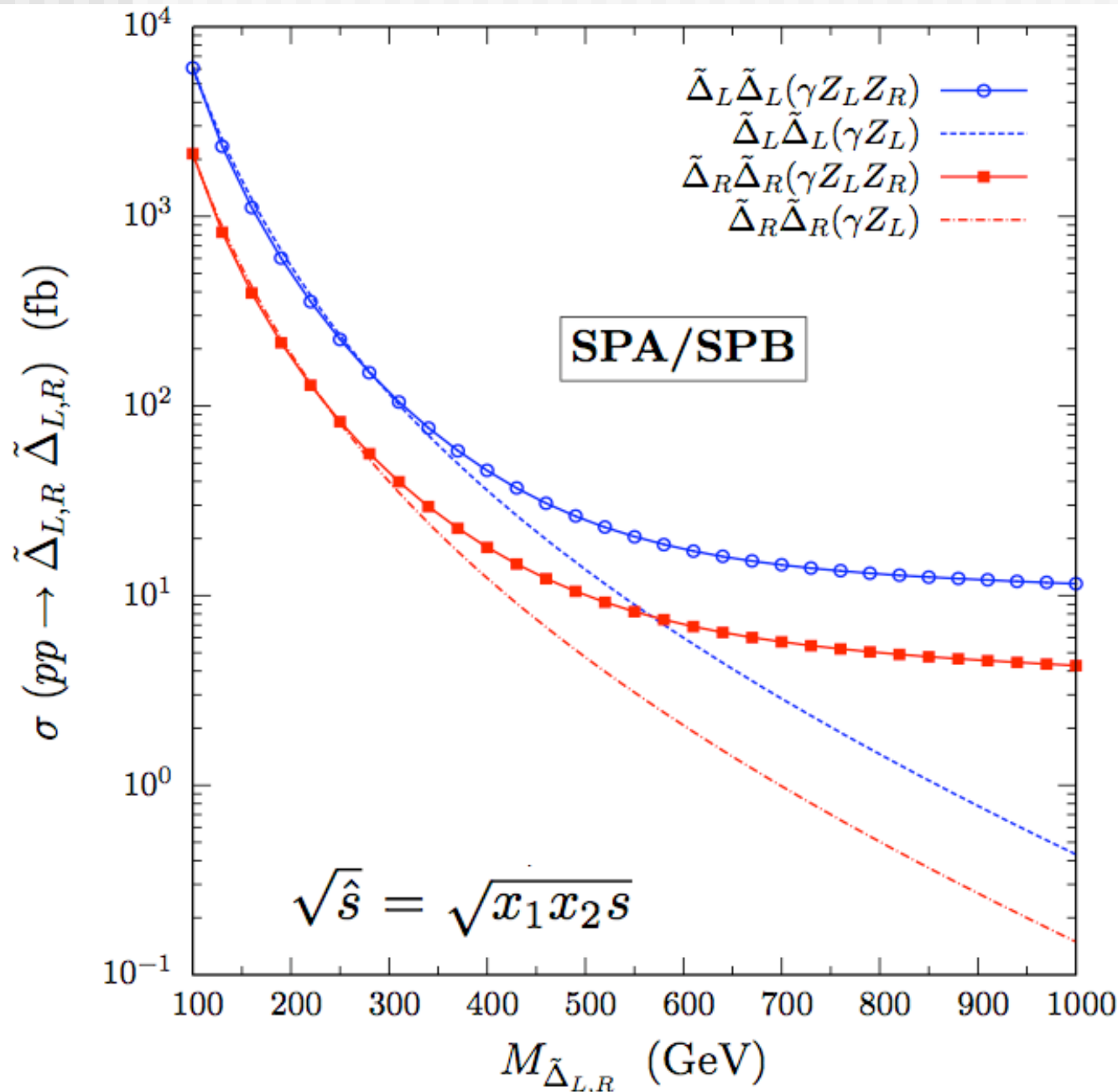
Fields	SPA	SPB
	$\tan \beta = 5, M_{B-L} = 25 \text{ GeV}$ $M_L = M_R = 250 \text{ GeV}$ $v_{\Delta_R} = 3000 \text{ GeV}, v_{\delta_R} = 1000 \text{ GeV}$ $\mu_1 = 1000 \text{ GeV}, \mu_3 = 300 \text{ GeV}$	$\tan \beta = 5, M_{B-L} = 100 \text{ GeV}$ $M_L = M_R = 500 \text{ GeV}$ $v_{\Delta_R} = 2500 \text{ GeV}, v_{\delta_R} = 1500 \text{ GeV}$ $\mu_1 = 500 \text{ GeV}, \mu_3 = 500 \text{ GeV}$
$\tilde{\chi}_i^0 \ (i = 1, 3)$	89.9, 180.6, 250.9 GeV	212.9, 441.2, 458.5 GeV
$\tilde{\chi}_i^\pm \ (i = 1, 3)$	250.9, 300.0, 953.9 GeV	459.4, 500.0, 500.0 GeV
$M_{\tilde{\Delta}}$	300 GeV	500 GeV
W_R, Z_R	2090.4, 3508.5 GeV	1927.2, 3234.8 GeV
	S2 S3	S2 S3
\tilde{e}_L, \tilde{e}_R	(156.9, 155.6 GeV), (402, 402 GeV)	(254.2, 253.4 GeV), (552, 552 GeV)
$\tilde{\mu}_L, \tilde{\mu}_R$	(156.9, 155.6 GeV), (402, 402 GeV)	(254.2, 253.4 GeV), (552, 552 GeV)
$\tilde{\tau}_1, \tilde{\tau}_2$	(155.4, 159.9 GeV), (401, 406 GeV)	(252.5, 257.9 GeV), (550, 556 GeV)

$$h_{ee} h_{\mu\mu} < 2.0 \times 10^{-7} \text{ GeV}^{-2} M_{\Delta}^2$$

from muonium-antimuonium transitions

4 lepton signals

$$pp \longrightarrow \tilde{\Delta}^{++} \tilde{\Delta}^{--} \longrightarrow (\ell_i^+ \ell_i^+) + (\ell_j^- \ell_j^-) + \cancel{E}_T$$



- cross section is quite sizeable for sufficiently light doubly charged Higgsinos $\sim 10^4$ fb
- The $4l + MET$ Signal receives contributions from the pair production of both chiral states of Δ .

4 lepton signals at LHC

- ♣ We have a rather clean and robust signal with highly suppressed SM background.*
- ♣ For tetralepton signals with a sufficiently large MET, SM background is estimated to be $\sim 10^{-3}$ fb.*
- ♣ This makes this channel highly promising for an efficient and clean disentanglement of LRSUSY effects.*
- ♣ Kinematic cuts:*
 $p_T^l > 25 \text{ GeV}; \quad |\eta_l| < 2.5$
 $\Delta R_{ll} > 0.4 \quad \& \quad E_T^{\text{miss}} > 50 \text{ GeV}$

4 lepton signals at LHC

- ♣ We use the CalcHEP+Pythia interface for numerical analysis.
- ♣ For the analysis we choose $(2\mu^- + 2e^+) + \text{MET}$ final state

♣ SPA:

$$\sigma(\tilde{\Delta}_L^{--}\tilde{\Delta}_L^{++}) = 117.9 \text{ fb}$$

$$\sigma(\tilde{\Delta}_R^{--}\tilde{\Delta}_R^{++}) = 44.5 \text{ fb.}$$

After cuts

$$- \text{S2} \quad \sigma(2\mu^- 2e^+ + \cancel{E}_T) = 7.71 \text{ fb,}$$

$$- \text{S3} \quad \sigma(2\mu^- 2e^+ + \cancel{E}_T) = 7.02 \text{ fb.}$$

♣ SPB:

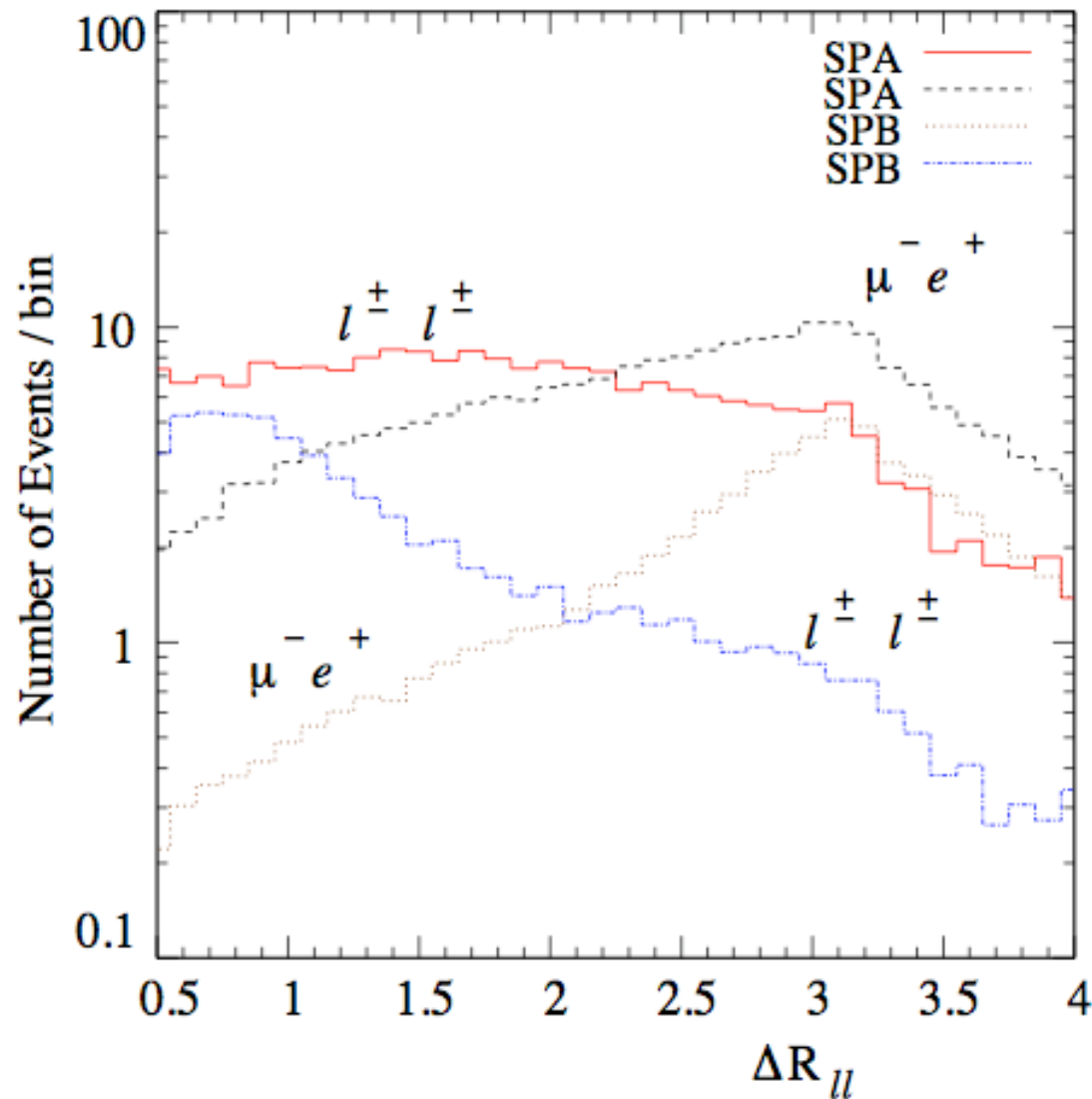
$$\sigma(\tilde{\Delta}_L^{--}\tilde{\Delta}_L^{++}) = 32.4 \text{ fb}$$

$$\sigma(\tilde{\Delta}_R^{--}\tilde{\Delta}_R^{++}) = 12.95 \text{ fb.}$$

$$- \text{S2} \quad \sigma(2\mu^- 2e^+ + \cancel{E}_T) = 2.43 \text{ fb,}$$

$$- \text{S3} \quad \sigma(2\mu^- 2e^+ + \cancel{E}_T) = 2.66 \text{ fb.}$$

4 lepton signals at LHC



- *SSSF leptons are peaked at lower values $\Delta R_{\ell\ell}$*

- *OSDF configurations are formed from two isolated leptons originating from separate cascades.*

For SPA: $M_{ll} = 209.6 \text{ GeV (S2)} , 210.1 \text{ GeV (S3)}$

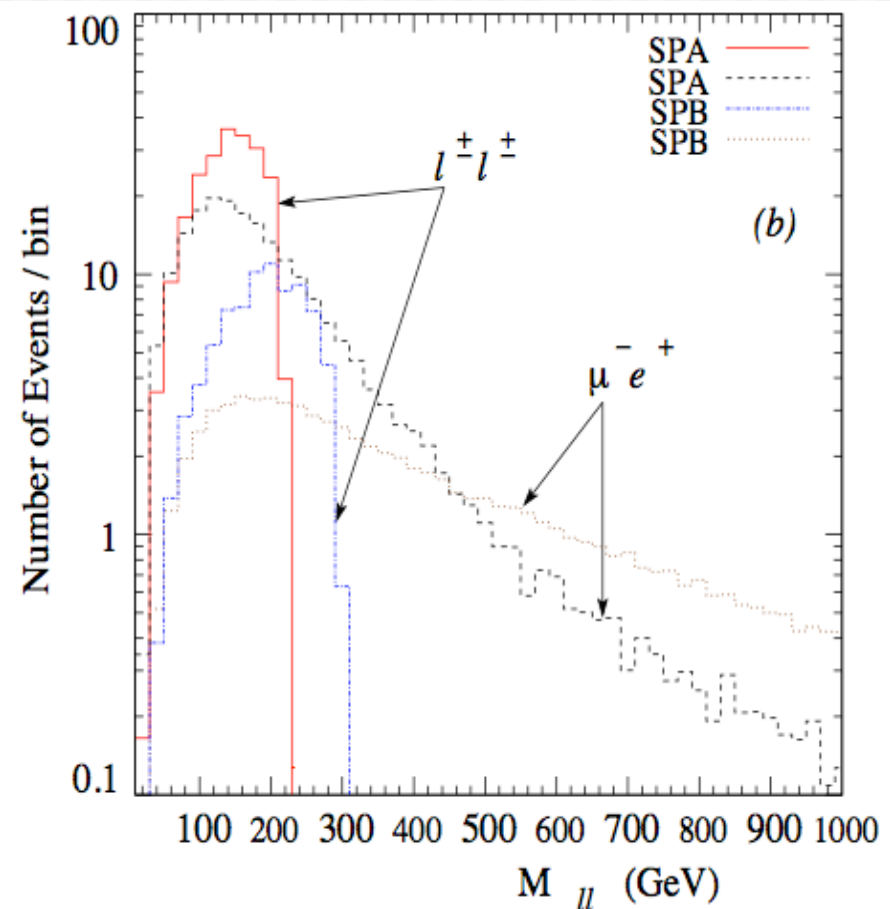
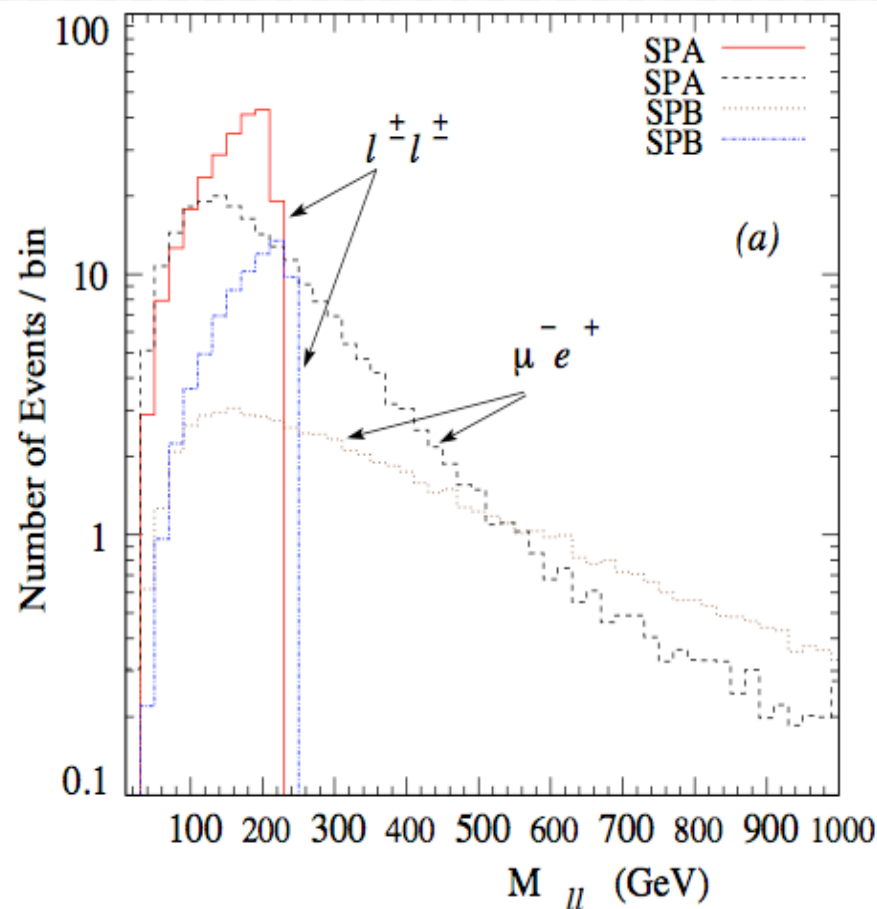
For SPB: $M_{ll} = 235.2 \text{ GeV (S2)} , 287.1 \text{ GeV (S3)}$

(S2)

$$M_{\ell^\pm \ell^\pm}^{max} = M_{\tilde{\Delta}} \sqrt{1 - \left(\frac{m_{\tilde{\ell}}}{M_{\tilde{\Delta}}}\right)^2} \sqrt{1 - \left(\frac{M_{\tilde{\chi}_1^0}}{m_{\tilde{\ell}}}\right)^2}$$

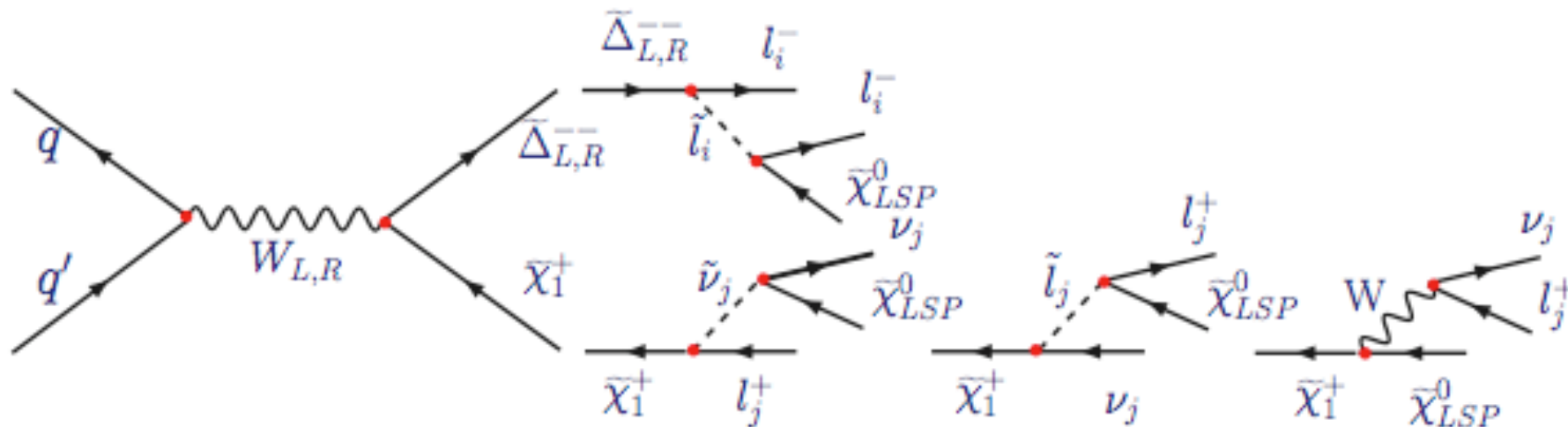
(S3)

$$M_{\ell^\pm \ell^\pm}^{max} = \sqrt{M_{\tilde{\Delta}}^2 + M_{\tilde{\chi}_1^0}^2 - 2M_{\tilde{\Delta}}E_{\tilde{\chi}_1^0}} ,$$



The edge in the SSSF dilepton invariant mass \rightarrow hint of a $\Delta L = 2$ interaction and a doubly charged particle in the underlying model of **new physics**.

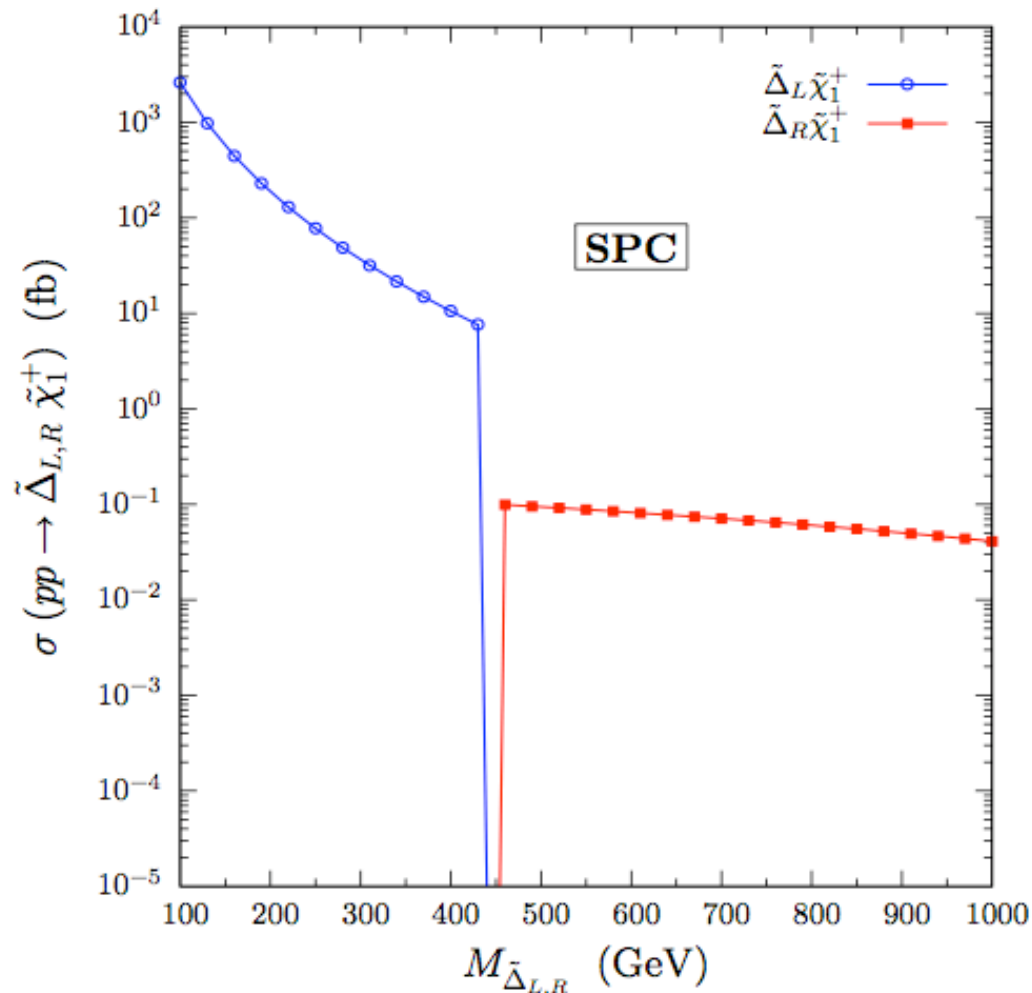
3 lepton signals:



	SPC
Fields	$\tan \beta = 5, M_{B-L} = 0 \text{ GeV}$ $M_L = M_R = 500 \text{ GeV}$ $v_{\Delta_R} = 2500 \text{ GeV}, v_{\delta_R} = 1500 \text{ GeV}$ $\mu_1 = 500 \text{ GeV}, \mu_3 = 300 \text{ GeV}$
$\tilde{\chi}_i^0 \ (i = 1, 3)$	142.5, 265.6, 300.0 GeV
$\tilde{\chi}_i^\pm \ (i = 1, 3)$	300.0, 459.3, 500.0 GeV
$M_{\tilde{\Delta}}$	300 GeV
W_R, Z_R	1927.2, 3234.8 GeV
	S2 S3
\tilde{e}_L, \tilde{e}_R	(214.9, 214.0 GeV), (402.6, 402.2 GeV)
$\tilde{\mu}_L, \tilde{\mu}_R$	(214.9, 214.0 GeV), (402.6, 402.2 GeV)
$\tilde{\tau}_1, \tilde{\tau}_2$	(212.8, 216.2 GeV), (401.5, 403.3 GeV)

3 lepton signals at LHC

$$pp \longrightarrow \tilde{\Delta}^{--} \tilde{\chi}_1^+ \longrightarrow (\ell_i^- \ell_i^-) + \ell_j^+ + \cancel{E}_T,$$



- Cross section small for SPA and SPB.
- SPC gives appreciable rates.
- Strongly depends on the composition of the lightest chargino.
- The dominant decay for chargino is slepton+neutrino~100%

Couplings:

$$\begin{aligned} \bullet W_L^\mu \tilde{\chi}_k^+ \tilde{\Delta}_L^{--} &: ig_L \gamma^\mu (V_{k5}^* P_L + U_{k5} P_R) \\ \bullet W_R^\mu \tilde{\chi}_k^+ \tilde{\Delta}_R^{--} &: ig_R \gamma^\mu (V_{k6}^* P_L + U_{k6} P_R) \end{aligned}$$

3 lepton signals at LHC

- ♣ *We use the similar cuts for the numerical analysis.*
- ♣ *For the analysis we choose $(2\mu^- + e^+) + \mathbf{MET}$ final state*

♣ *SPC:*

$$\sigma(\tilde{\Delta}_L^{--} \tilde{\chi}_1^+) = 36.57 \text{ fb},$$

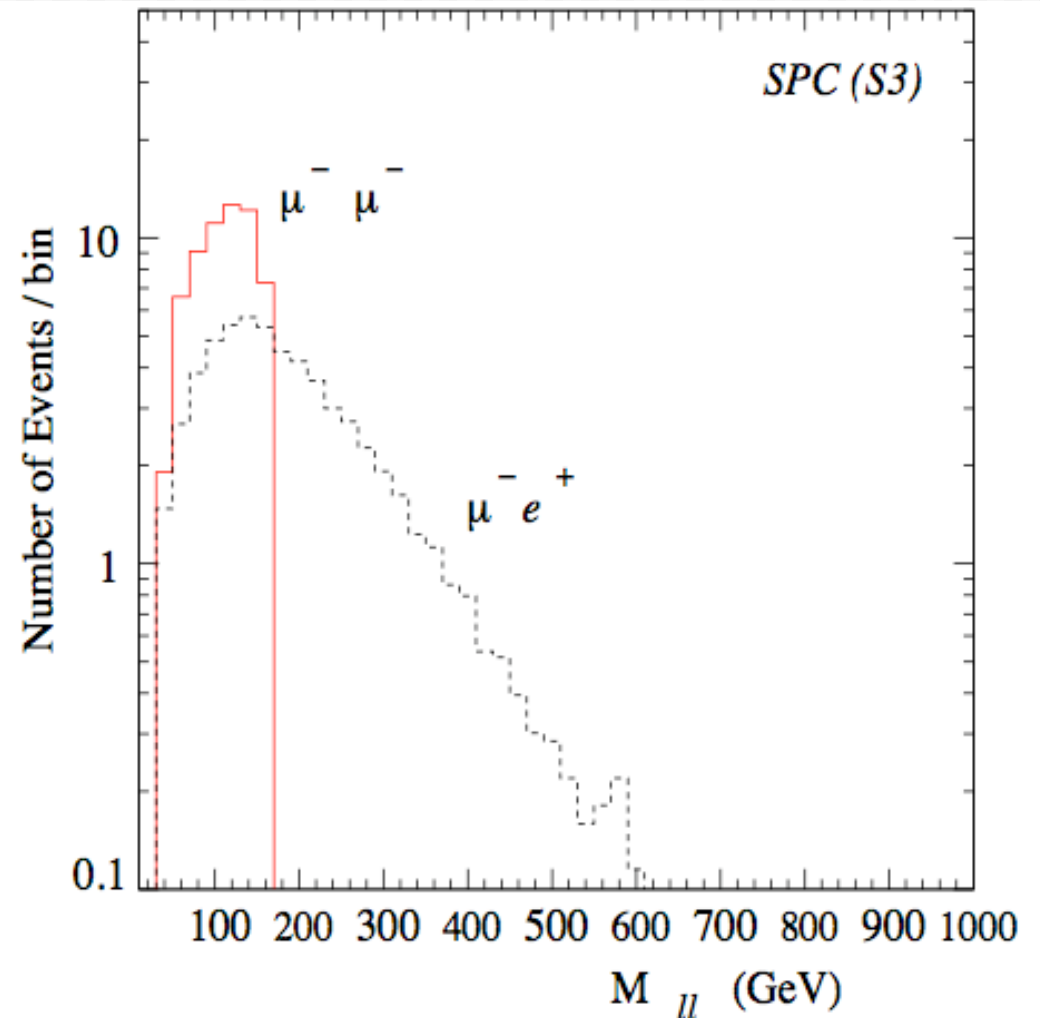
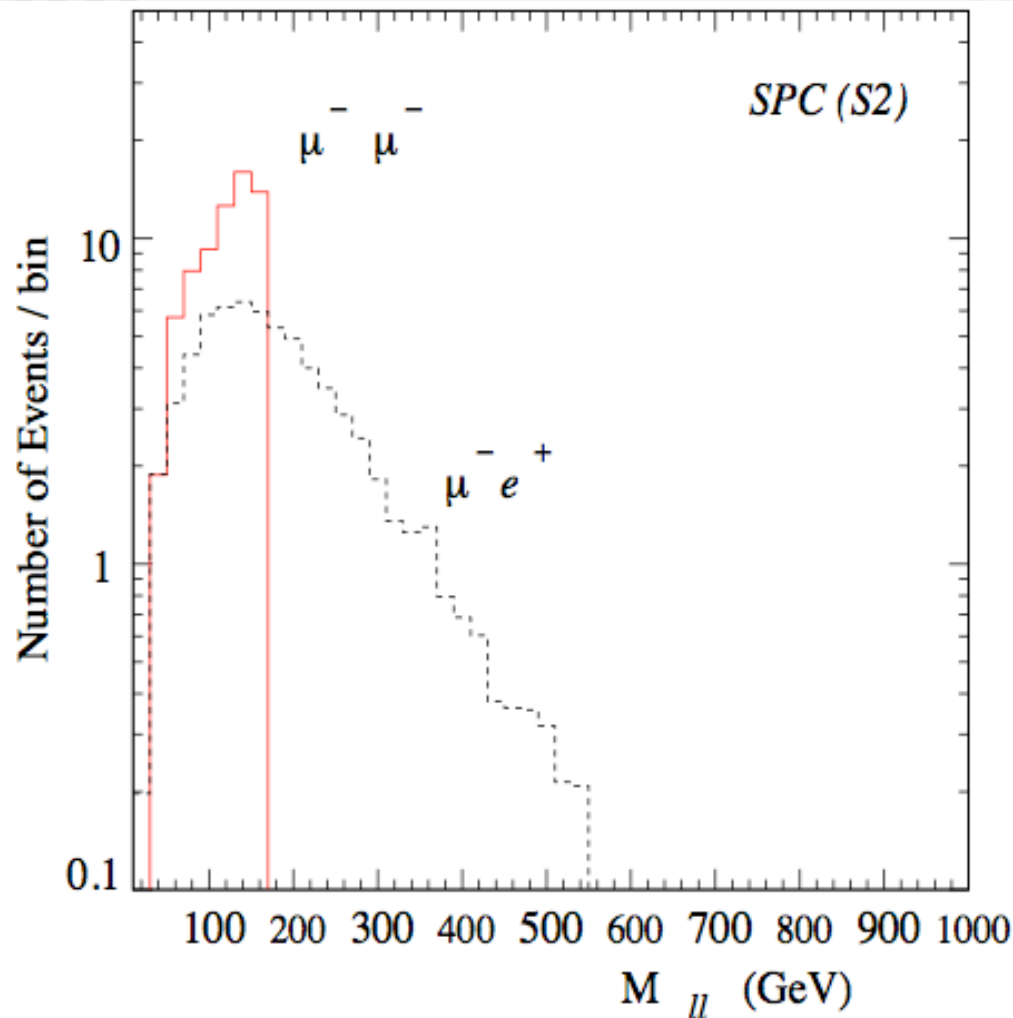
After cuts

$$\begin{aligned} - \text{S2} \quad & \sigma(2\ell_i^- \ell_j^+ \cancel{E}_T) = 2.24 \text{ fb}, \\ - \text{S3} \quad & \sigma(2\ell_i^- \ell_j^+ \cancel{E}_T) = 2.03 \text{ fb}, \end{aligned}$$

- ♣ *Relatively similar kinematic distributions for the SSSF and OSDF dilepton pairs.*

3 lepton signals at LHC

For SPC: $M_{ll} = 156.7 \text{ GeV (S2)}$, 157.5 GeV (S3)



Distinguishing power at LHC

- ♣ *The $4l+MET$ signal is an excellent option to achieve this.*
- ♣ *Once we make the choice $l_i \neq l_j$ we have two pairs SSSF dileptons in the final state. $--> (2\mu^- + 2e^+)$*

hard to think of “standard” SUSY or UED giving this. Possible if all 4 leptons are identical flavor.

(In SUSY/UED χ_2 / Z_1 pair production)
$$\chi_2 --> \chi_1 l^+ l^- ; Z_1 --> \gamma_1 l^+ l^-$$

The invariant mass distribution for the SSSF dilepton (or OSSF) and the $\Delta \mathbf{R}_{ll}$ distribution would prove to be a good discriminant.

Distinguishing power at LHC

♣ *possibilities with two different flavours..*

-- *pair production of doubly charged scalars*

(invariant mass distribution for SSSF dilepton should give a sharp peak --> scalar mass)

-- *heavy right-handed neutrinos ($N \rightarrow l_i W \rightarrow l_i l_j + MET$)*

♣ *Discrimination also possible for trilepton signals following similar arguments.*

Conclusions

- ★ *The left-right supersymmetric theories predict light doubly charged Higgsinos.*
- ★ *We show that production cross section for doubly charged Higgsinos in LRSUSY framework is large at LHC.*
- ★ *$4l+MET$ and $3l+MET$ signal at LHC gives robust signatures in the form of SSSF dileptons.*
- ★ *Kinematic distributions prove to be very good discriminants from signals coming from other new physics scenarios.*

Conclusions

- ★ *The presence of $\Delta L=2$ processes in theories beyond the SM can be probed at colliders.*
- ★ *Extended gauge and Higgs sector gives more interesting possibilities for collider searches in the LRSUSY model.*

Extra Slides

- $\tilde{\Delta}_L^{--} \tilde{l} l :$ $-2h_{ll}\mathcal{C}^{-1}P_L$
- $\tilde{\Delta}_R^{--} \tilde{l} l :$ $-2h_{ll}\mathcal{C}^{-1}P_R$

Fermion-Fermion-Z Boson, γ :

- $\gamma^\mu \tilde{\Delta}_{L,R}^{--} \tilde{\Delta}_{L,R}^{--} :$ $2ie\gamma^\mu$
- $Z_L^\mu \tilde{\Delta}_L^{--} \tilde{\Delta}_L^{--} :$ $i \frac{g_L \cos 2\theta_W}{\cos \theta_W} \gamma^\mu$
- $Z_L^\mu \tilde{\Delta}_R^{--} \tilde{\Delta}_R^{--} :$ $-i \frac{2g_L \sin^2 \theta_W}{\cos \theta_W} \gamma^\mu$
- $Z_R^\mu \tilde{\Delta}_L^{--} \tilde{\Delta}_L^{--} :$ $i \frac{g_L \sqrt{\cos 2\theta_W}}{\cos \theta_W} \gamma^\mu$
- $Z_R^\mu \tilde{\Delta}_R^{--} \tilde{\Delta}_R^{--} :$ $-i \frac{g_L (1 - 3 \sin^2 \theta_W)}{\cos \theta_W \sqrt{\cos 2\theta_W}} \gamma^\mu$

- $\tilde{\chi}_k^0 \tilde{l} \bar{l} :$ $-i \left\{ \left[\sqrt{2}g_L \left(\frac{1}{2}N_{k1} - \frac{1}{2} \left(\frac{\cos 2\theta_W}{\cos^2 \theta_W} + \tan^2 \theta_W \right) N_{k2} - \frac{\sin \theta_W \sqrt{\cos 2\theta_W}}{\cos^2 \theta_W} N_{k3} + \frac{m_l}{2M_W \cos \beta} N_{k5} \right) \right] P_L \right.$
 $\left. - \left[\sqrt{2}g_R \left(\left(\frac{\cos 2\theta_W}{2 \cos^2 \theta_W} - \tan^2 \theta_W \right) N_{k2} - \frac{\sin \theta_W \sqrt{\cos 2\theta_W}}{\cos^2 \theta_W} N_{k3} + \frac{m_l}{2M_W \cos \beta} N_{k5}^* \right) \right] P_R \right\}$
- $\tilde{\chi}_k^0 \tilde{\nu} \bar{\nu} :$ $-i \left\{ \left[\sqrt{2}g_L \left(\frac{1}{2}N_{k1} + \frac{1}{2} \left(\frac{\cos 2\theta_W}{\cos^2 \theta_W} - \tan^2 \theta_W \right) N_{k2} - \frac{\sin \theta_W \sqrt{\cos 2\theta_W}}{\cos^2 \theta_W} N_{k3} + \frac{m_l}{2M_W \cos \beta} N_{k5} \right) \right] P_L \right.$
 $\left. - \left[\sqrt{2}g_R \left(\frac{\cos 2\theta_W}{2 \cos^2 \theta_W} N_{k2} - \frac{\sin \theta_W \sqrt{\cos 2\theta_W}}{2 \cos^2 \theta_W} N_{k3} + \frac{m_l}{2M_W \cos \beta} N_{k5}^* \right) \right] P_R \right\}$

Bounds on the Yukawa couplings

$$h_{e\mu}h_{ee} < 3.2 \times 10^{-11} \text{ GeV}^{-2} \cdot M_{\Delta^{--}}^2 \quad \text{from } \mu \rightarrow \bar{e}ee,$$

$$h_{e\mu}h_{\mu\mu} < 2 \times 10^{-10} \text{ GeV}^{-2} \cdot M_{\Delta^{--}}^2 \quad \text{from } \mu \rightarrow e\gamma,$$

$$h_{ee}^2 < 9.7 \times 10^{-6} \text{ GeV}^{-2} \cdot M_{\Delta^{--}}^2 \quad \text{from Bhabha scattering,}$$

$$h_{\mu\mu}^2 < 2.5 \times 10^{-5} \text{ GeV}^{-2} \cdot M_{\Delta^{--}}^2 \quad \text{from } (g-2)_\mu,$$

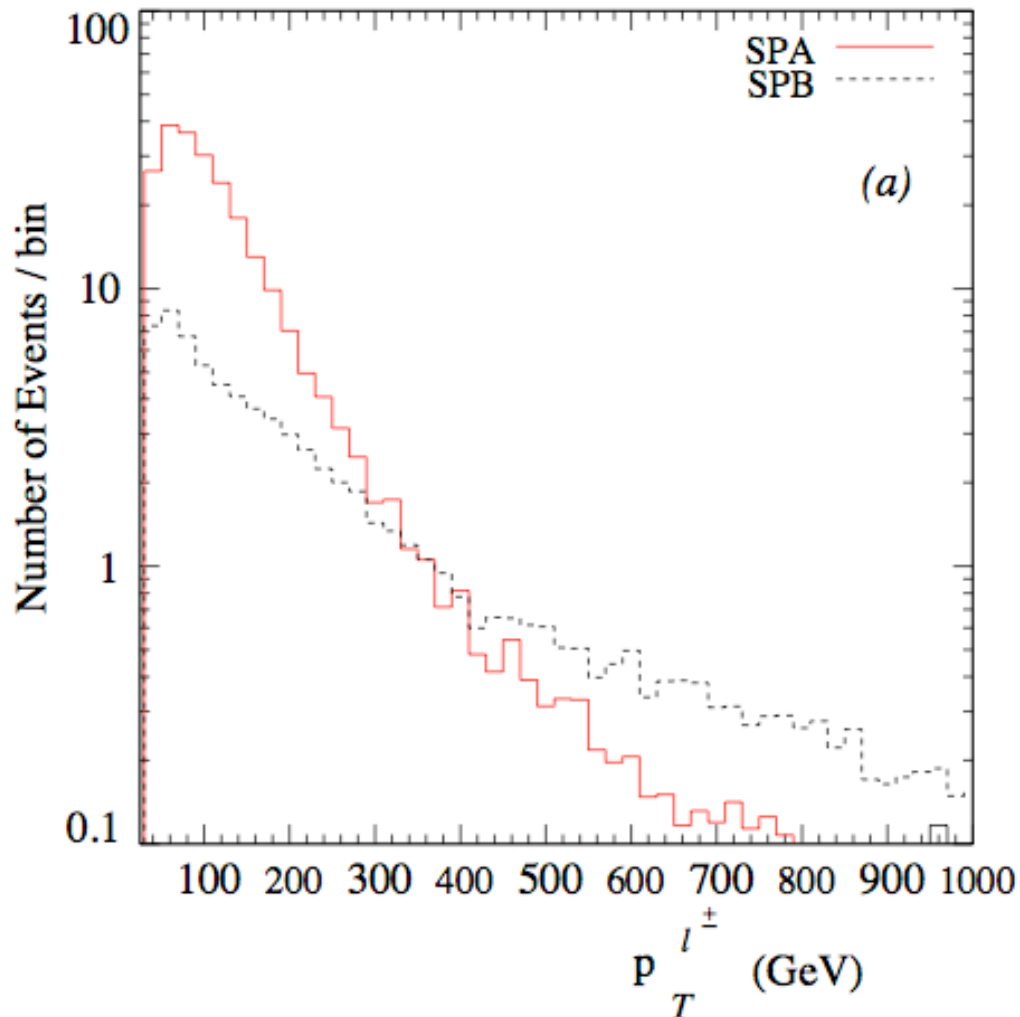
$$h_{ee}h_{\mu\mu} < 2.0 \times 10^{-7} \text{ GeV}^{-2} \cdot M_{\Delta^{--}}^2 \quad \text{from muonium - antimuonium transition.}$$

We choose $\mathbf{h}_{II} = 0.1$ which is consistent with the bounds.
Larger values allowed with a large mass for Δ^{--}

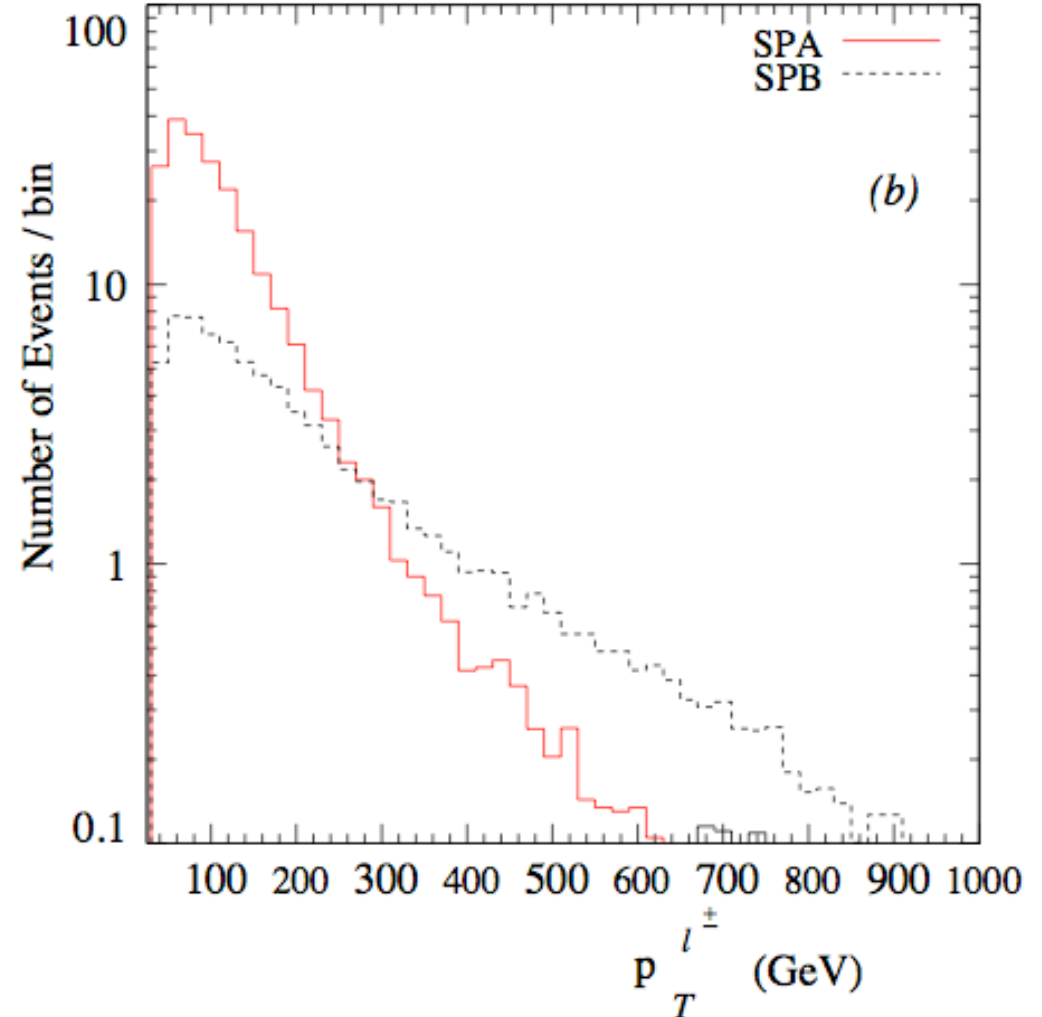
4 lepton signals at LHC

The p_T distribution for the charged leptons

(S2)



(S3)



The mixing matrix for sleptons

$$\mathcal{M}_L^2 = \begin{pmatrix} M_{LL}^2 & M_{LR}^2 \\ M_{RL}^2 & M_{RR}^2 \end{pmatrix}$$

where the different entries correspond to

$$\begin{aligned} M_{LL}^2 &= M_L^2 + m_\ell^2 + m_Z^2 (T_{3\ell} + \sin^2 \theta_W) \cos 2\beta, \\ M_{LR}^2 &= M_{RL}^{2\dagger} = m_\ell (A + \mu \tan \beta), \\ M_{RR}^2 &= M_R^2 + m_\ell^2 - m_Z^2 \sin^2 \theta_W \cos 2\beta \end{aligned}$$